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GNSS



SENTINEL-3A/3B

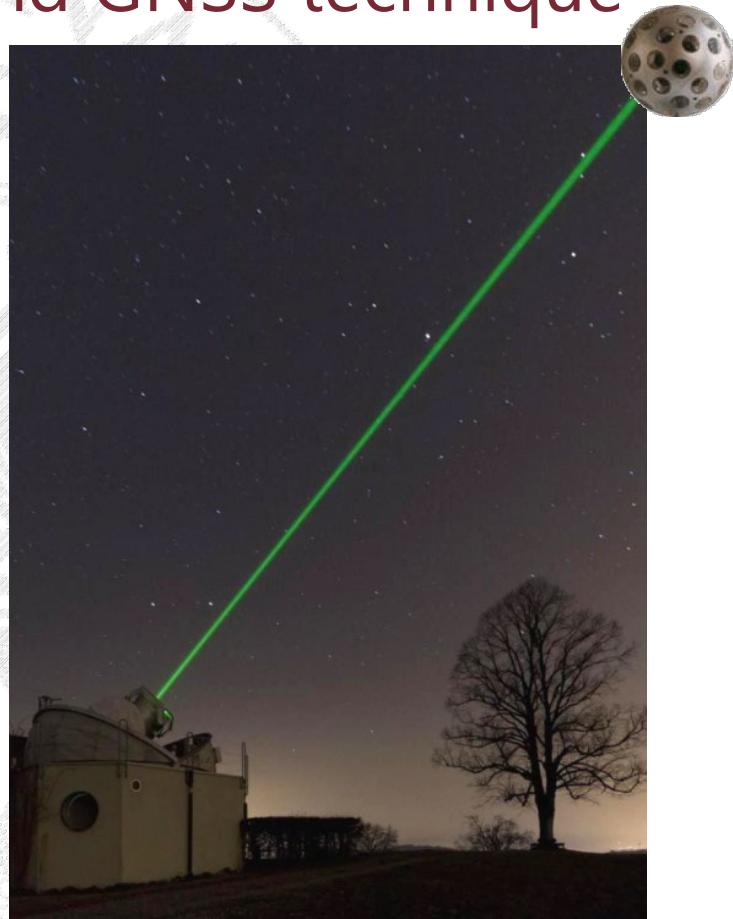


LAGEOS 1/2

**Determination of global geodetic parameters and station coordinates based on SLR measurements to reduced-dynamic Sentinel-3A/3B orbits**

**Dariusz Strugarek**

# SLR and GNSS technique



## Satellite Laser Ranging (SLR)

optical technique based on registration of time-of-flight of laser signal, from station telescopes to the retroreflector mounted on a satellite, where a laser pulse is reflected back to the detector at the station.



## Global Navigational Satellite Systems (GNSS)

active satellite technique based on microwave signal from satellite to receivers in positioning. GNSS use satellite signals from global and regional navigation satellite systems

# Sentinel-3A/B



## Sentinel-3A/3B

- ESA and EUMETSAT
- active satellite
- ocean surface topography
- land and ocean temperature and color measurements
- climate and environment changes monitoring
- polar, sun-synchronous, circular orbit
- equipped with retroreflectors dedicated for SLR technique, DORIS and GNSS receivers

Sentinel info	3A	3B
Start	16-Feb-2016	25-Apr-2018
End	After 7 years	
Altitude	815 km	
Inclination	98.65°	
Weight	1150 kg	
Earth coverage	27 days	

# LAGEOS 1/2



## LAGEOS, LAGEOS-2

(LAsEr GEOdynamics Satellite or LAsEr GEOdetic Satellite)

- NASA and ASI
- used for relativistic effects, gravity field, geodynamics, ERP, geocenter coordinates research by SLR measurements

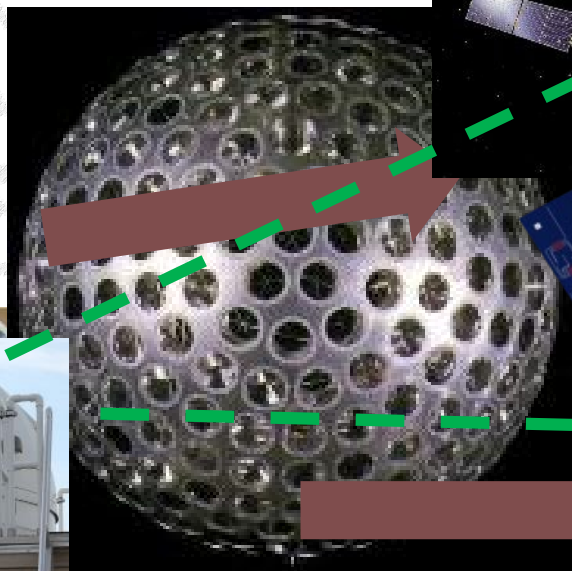
LAGEOS info	1	2
Start	04-May-1976	22-Oct-1992
End	-	-
Altitude	5850 km	5625 km
Inclination	109.84°	52.64°
Weight	406.965 kg	405.380 kg
Period	225 min	223 min
Orbit	circular	

- passive, spherical, geodetic satellites, with low Area-to-mass ratio
- equipped with 426 retroreflectors dedicated for SLR technique

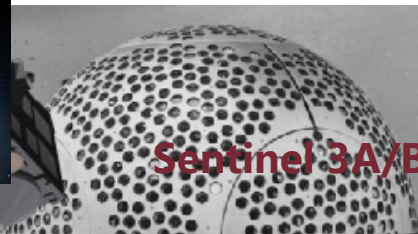
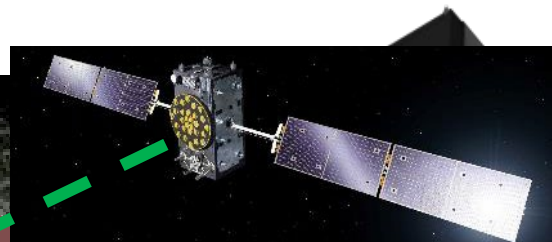
# Motivation



retroreflectors



LAGEOS 1/2



Sentinel 3A/B



GNSS

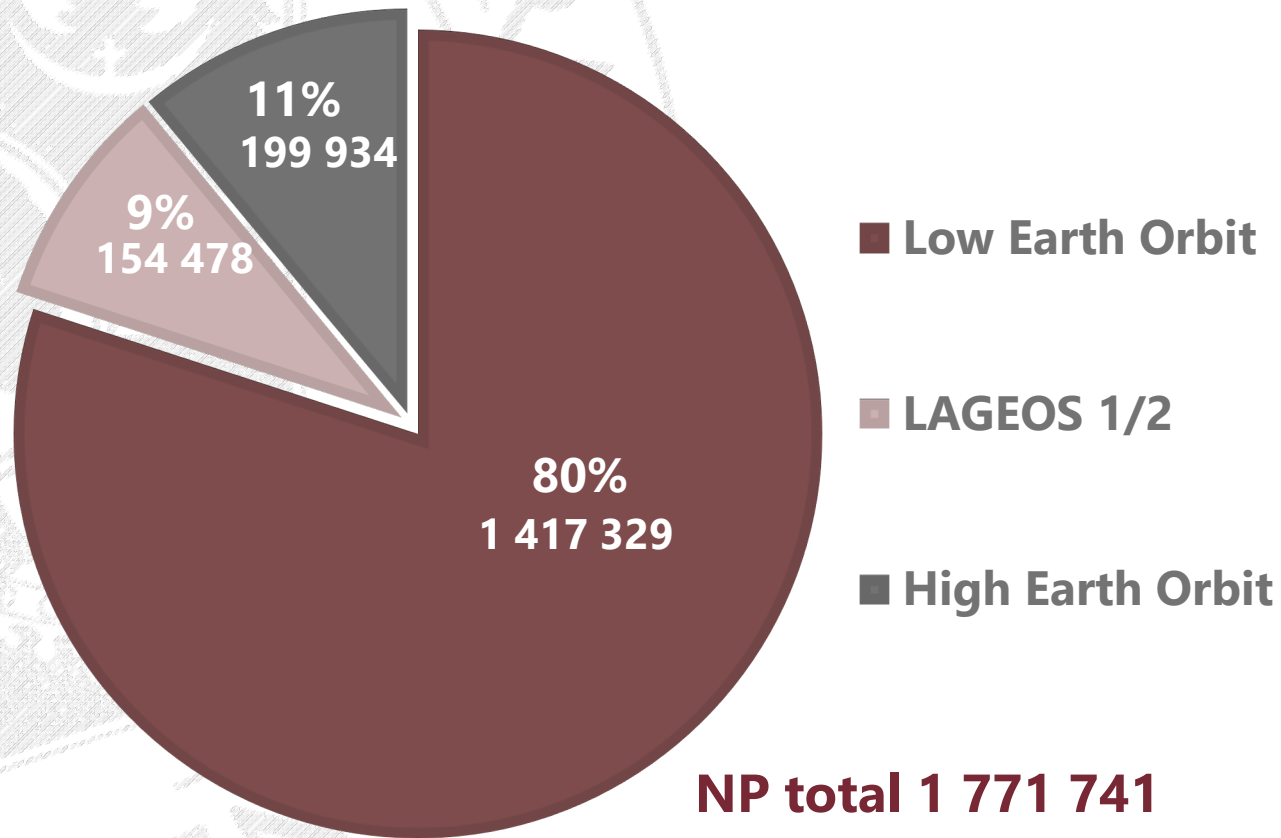
- ITRF
- GEOCENTER
- ERP

?

International Reference Frame (IRF) center (2014-2018) interworking with GNSS and Earth rotation parameters (ERP) to determine the Earth's center of mass and Earth rotation parameters. For the realization of reference frames (e.g. SRF2014) coordinates and Earth rotation parameters

# SLR observations

## PERCENTAGE/NUMBER OF SLR OBSERVATIONS (NORMAL POINTS) TO PARTICULAR SATELLITE TYPE IN 2017



Just 9 % of all SLR measurements are used for reference frames realization, determination of Earth rotation parameters, geocenter coordinates

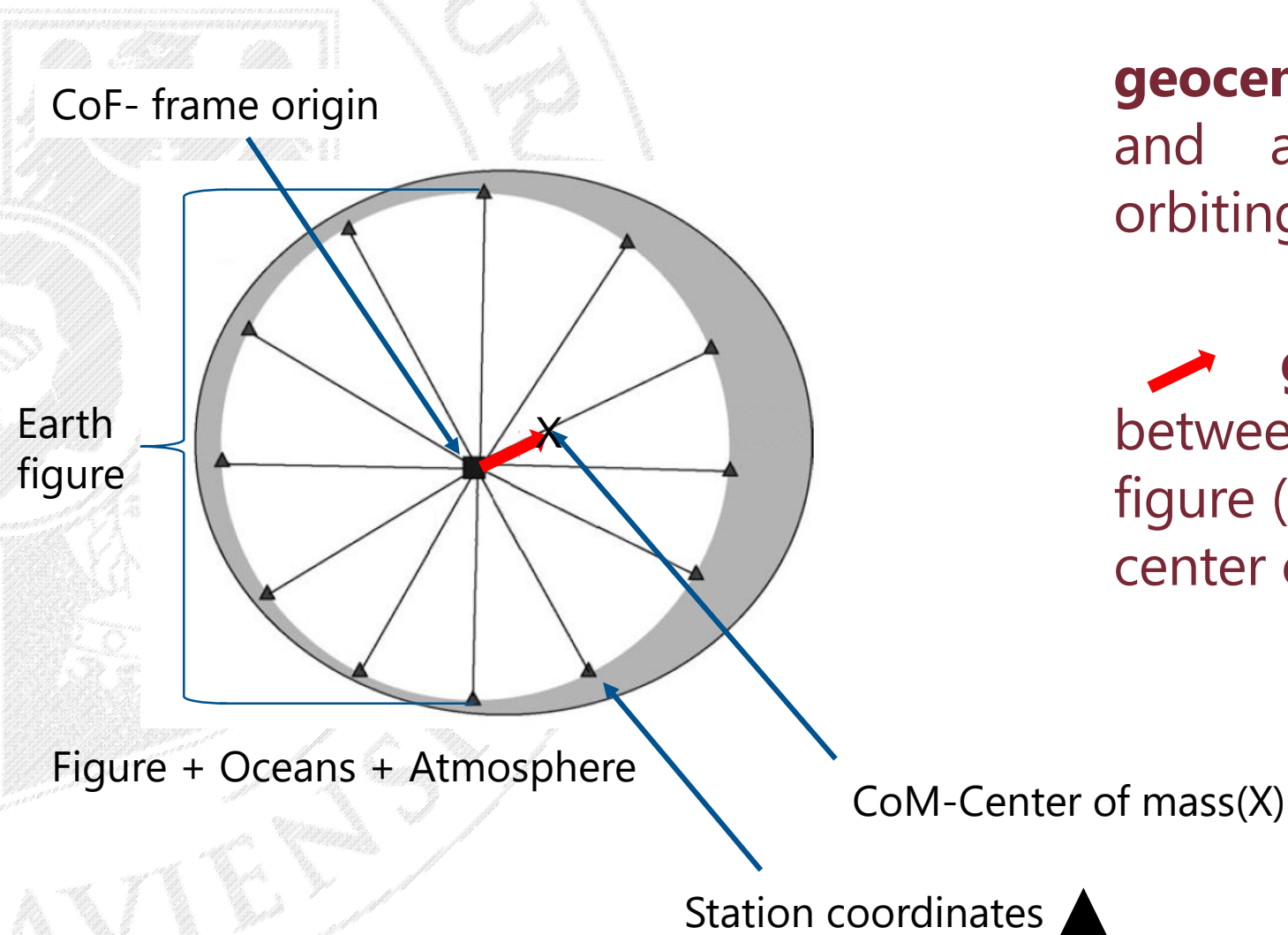
HEO = GNSS (MEO+IGSO+GEO)

# Parameters

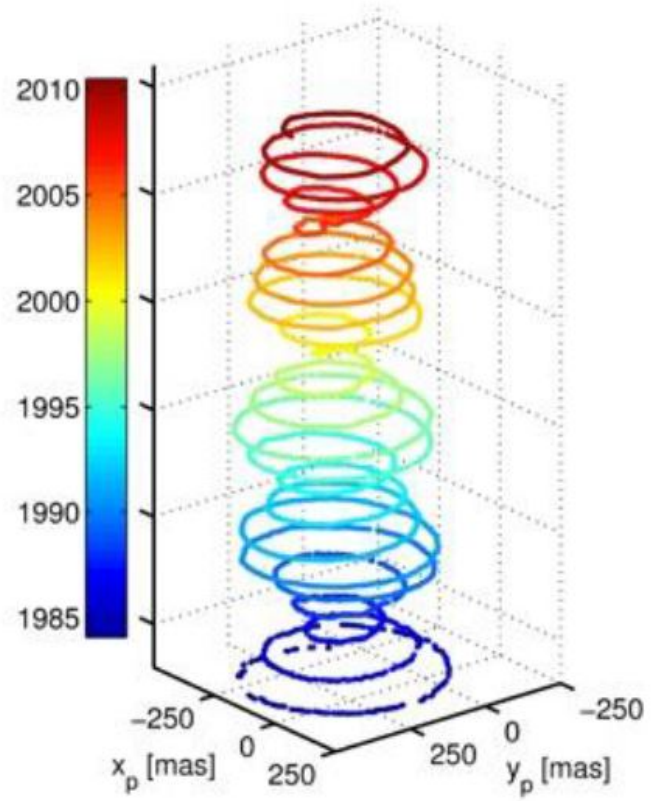
**SLR sites coordinates** (XYZ for e.g. ITRF2014, SLRF2014; North, East, Up dla IGS14)

**geocenter-** center of Earth mass with ocean and atmosphere layers, CoM), satellites orbiting point

**geocenter movement** - vector between frame origin-Center of the Earth figure (CoF, based on station coordinates) and center of mass



# Parameters



Pole coordinates

## Pole coordinates (X,Y)

difference between the Earth rotation axis orientation and reference coordinates (based on IERS Reference Pole (IRP) conventions)

## Length of day, UT1-UTC parameter,

difference between universal time (mean solar time on the Prime Meridian at Greenwich) and Universal Time Coordinated (time scale consistent with TAI-International Atomic Time), first derivative of UT1-UTC = Length of day (LoD)



## SLR measurements

**Active satellites:** own power source, communication devices, solar panels different shape, weight, equipment, eg. SENTINEL 3A/B

**Passive satellites:** no power source, communication, research devices, weight, shape and surface dedicated for orbit perturbation reduction, e.g. LAGEOS 1/2

**SLR**



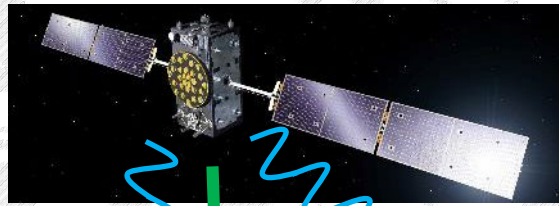
**GNSS, LEO orbits validation**

**SLR**



**Station coordinates, geocenter coordinates, ERP, scale, relativistic effects determination**

# Sentinel 3A/B GNSS- and SLR- based analysis

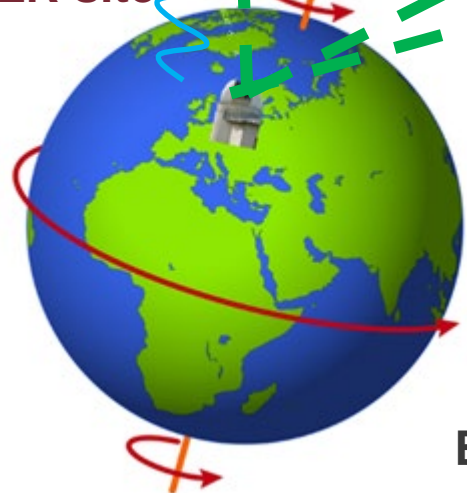


**GNSS**

**Sentinel 3A/B LAGEOS**



**SLR site**



--- laser  
~ microwave

SLR  
normal  
points



High-quality GNSS orbit  
and orientation data  
(ambiguity solution, orbit  
correction by AIUB)

**geodetic satellites  
likewise approach**



Station CRD  
Geocenter CRD

ERP's  
Station errors (biases)



**Combined Sentinel 3A + LAGEOS Solution  
„SLR-PPP”**

# Solution tests– SLR to Sentinel-3A/B

Sentinel-3A/3B  
(fixed GPS-based orbits)



## Solution tests: different network and parameters constraining and different number of accumulated 1-day orbit combination

**Test1:** network constraining: no-net-translation (NNT) no-net-rotation(NNR) with estimation of parameters



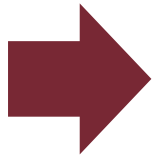
Station coordinates  
Geocenter coordinates  
ERP

**Test2:** network constraining: no-net-translation (NNT) no-net-rotation(NNR) without estimation of parameters



Station coordinates

**Test3:** no network constraining and without estimation of parameters



Station coordinates  
SLR-PPP'

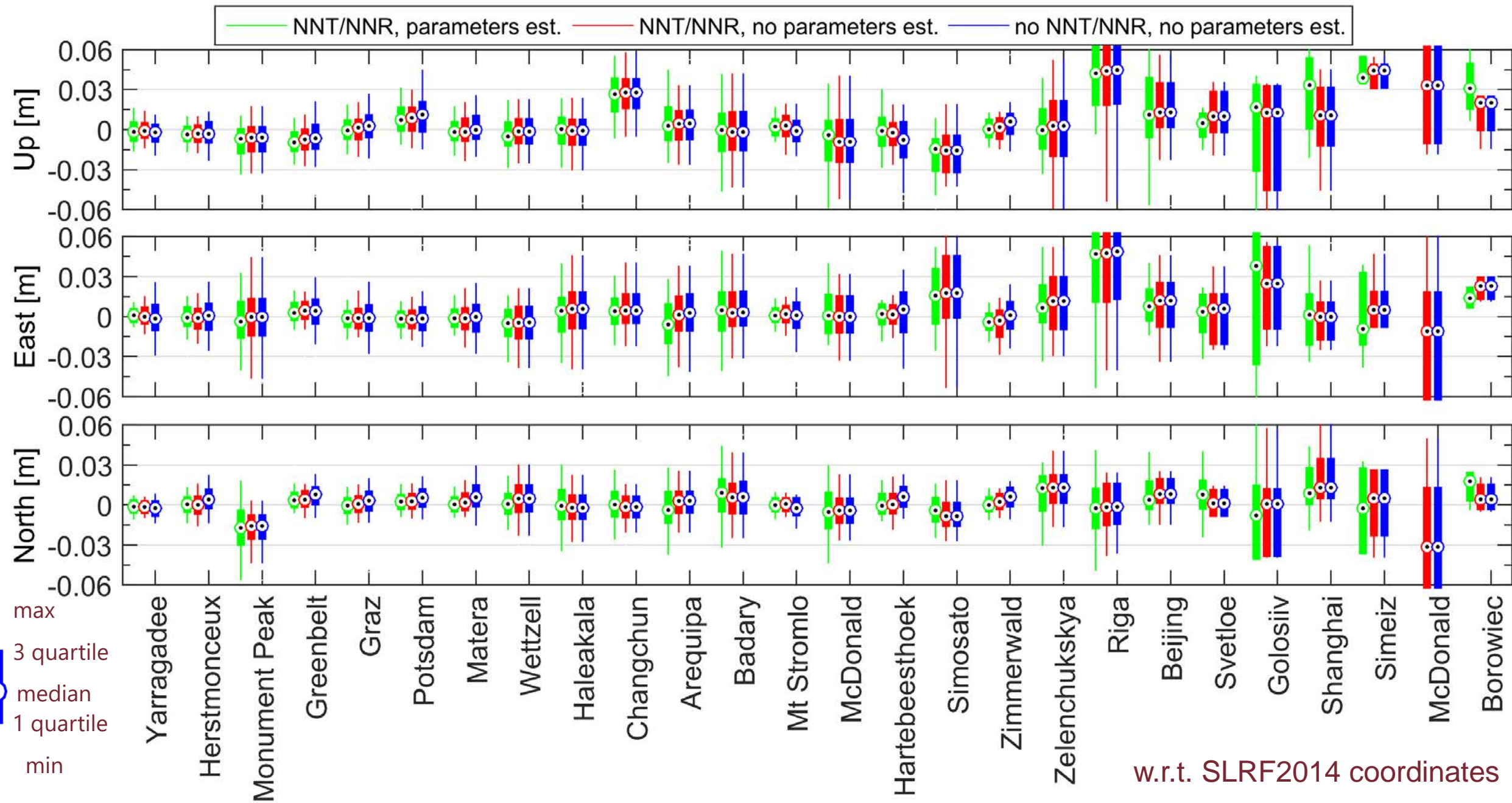


## Solution tests– SLR to Sentinel-3A/B

### **Solution tests: different network and parameters constraining and different number of accumulated 1-day orbit combination**

- Station coordinates 1-, 3-, 7-, 15- accumulation of 1-day orbits
- Geocenter coordinates: 3-, 5-, 7- accumulation of 1-day orbits
- ERP : 3-, 5-, 7- accumulation of 1-day orbits

# Constraining tests– Sentinel-3A/B



# Different number of accumulated 1-day orbit

Coordinates	Up [mm]				North [mm]				East [mm]			
1-orbit No.	1	3	7	15	1	3	7	15	1	3	7	15
IQR	31.3	17.8	<b>16.3</b>	<b>14.7</b>	15.6	12.1	<b>11.7</b>	<b>9.4</b>	24.9	14.6	<b>13.4</b>	<b>11.0</b>
Median	0.7	-0.5	<b>-0.7</b>	<b>-0.9</b>	0.2	-0.4	<b>0.0</b>	<b>0.1</b>	0.4	0.1	<b>0.2</b>	<b>0.2</b>

Station CRD

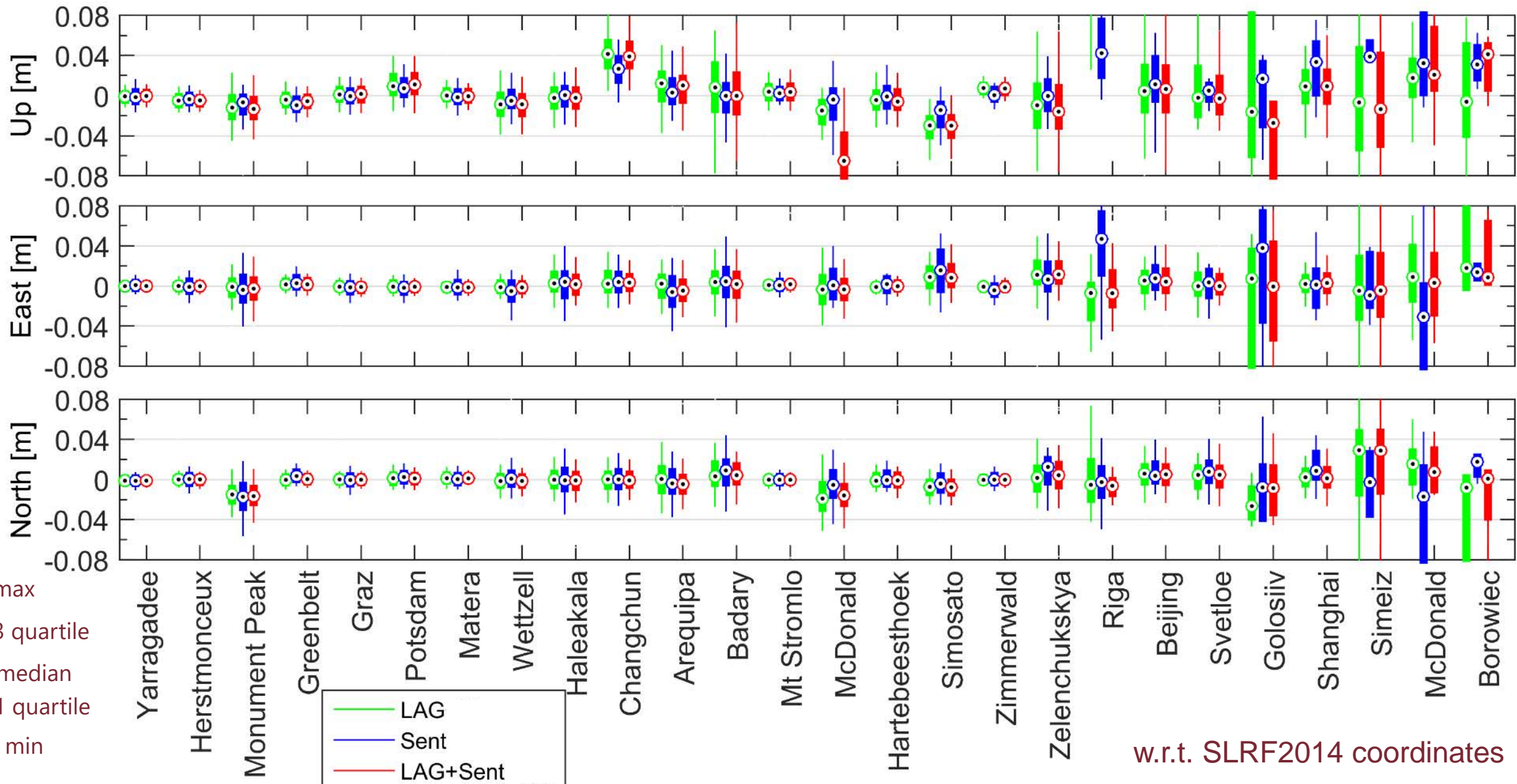
Coordinates	X [mm]			Y [mm]			Z [mm]		
1-orbit No.	3	5	7	3	5	7	3	5	7
RMS	16.4	14.4	<b>6.5</b>	10.2	9.5	<b>4.2</b>	16.7	14.6	<b>6.0</b>
Mean	-1.9	-1.5	<b>-1.2</b>	1.8	0.5	<b>0.5</b>	-4.1	-5.6	<b>-1.3</b>

Geocenter CRD

Parameters	X pole [mas]			Y pole [mas]			dT [ms/day]		
1-orbit No.	3	5	7	3	5	7	3	5	7
RMS	0.80	0.56	<b>0.32</b>	1.14	0.83	<b>0.32</b>	0.10	0.07	<b>0.06</b>
Mean	0.06	0.06	<b>0.11</b>	0.20	0.16	<b>0.04</b>	-0.0020	0.0022	<b>-0.0023</b>

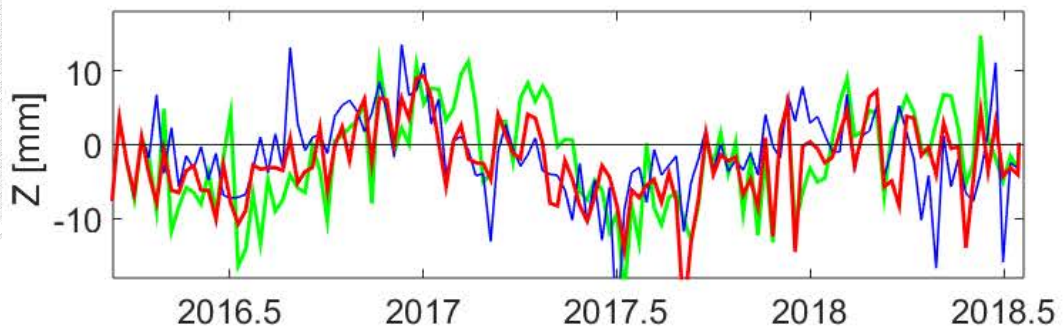
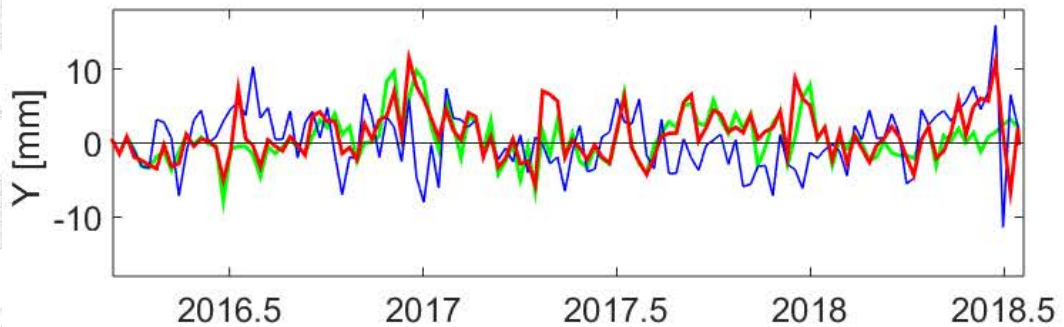
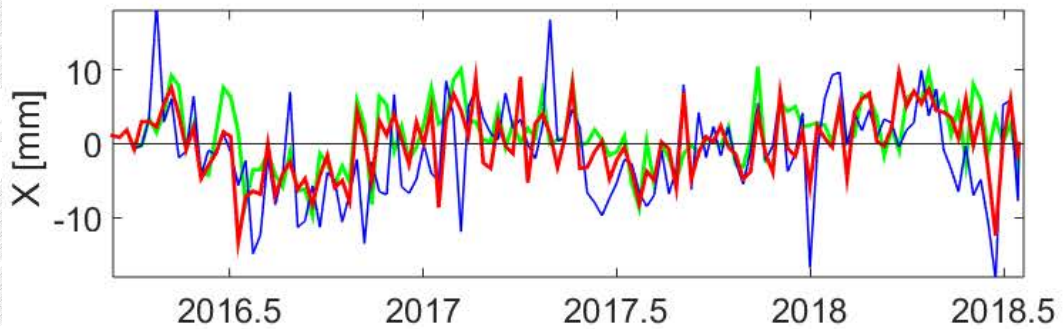
Pole CRD i LoD

# Combined Sentinels-3A/B+LAGEOS solution

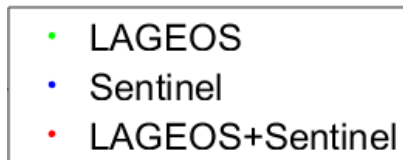


w.r.t. SLRF2014 coordinates

# Combined Sentinels-3A/B+LAGEOS solution, geocenter

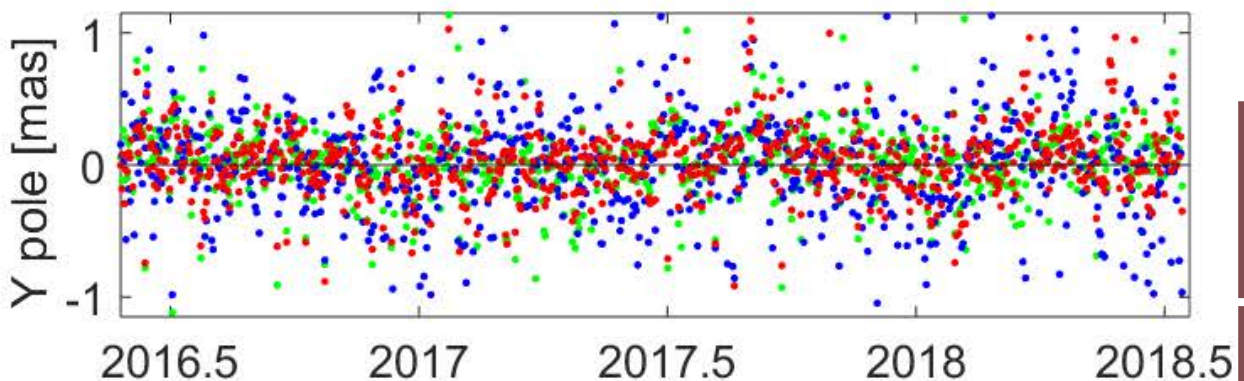
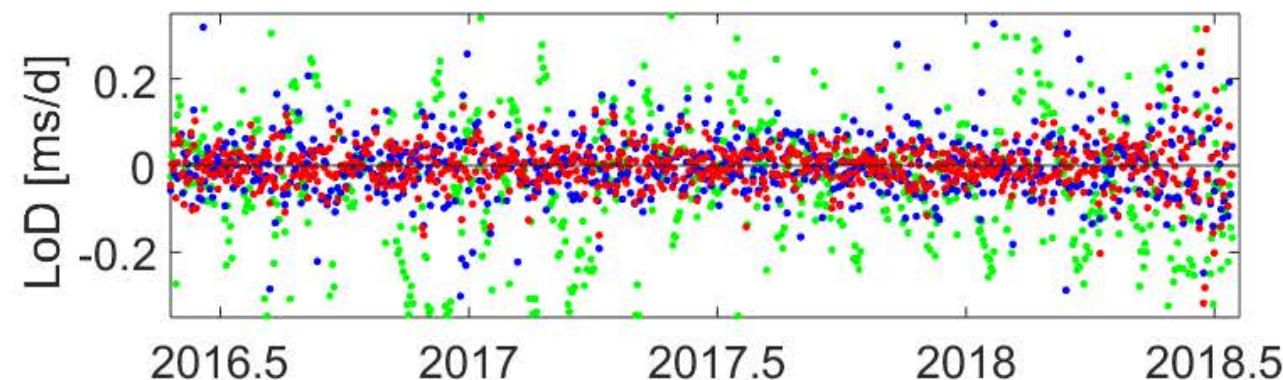
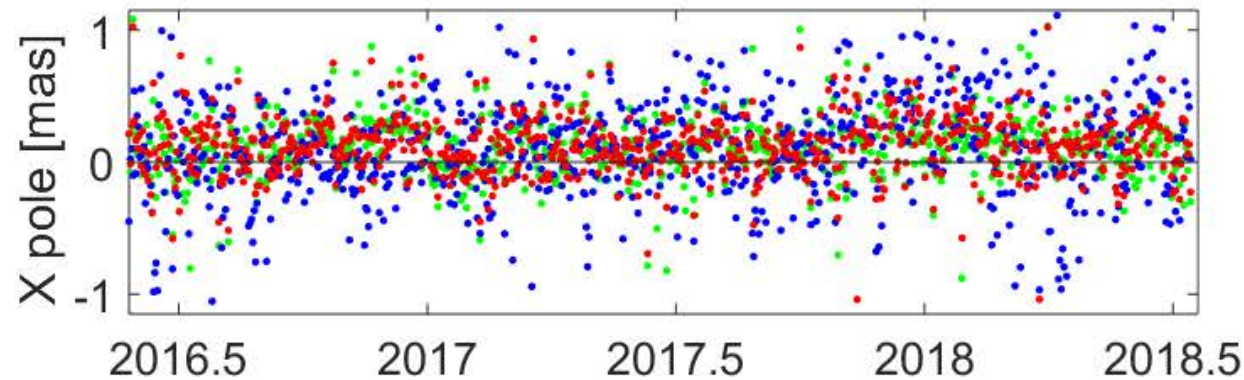


Differences	LAG-SENT	LAG-(LAG+SENT)	SENT-(LAG+SENT)
	std [mm]	std [mm]	std [mm]
X	6.2	3.6	5.1
Y	5.0	2.4	4.7
Z	7.1	4.5	5.1





# Combined Sentinels-3A/B+LAGEOS solution, ERP



Solution	X pole [mas]		Y pole [mas]		LOD [ms/day]	
	mean	RMS	mean	RMS	mean	RMS
LAG	0.128	0.134	0.047	0.166	-0.098	0.107
Sent	0.109	0.320	0.040	0.314	-0.002	<b>0.063</b>
LAG+Sent	0.134	0.138	0.044	0.189	-0.011	<b>0.067</b>

w.r.t. C04 parameters (IERS data)

# Summary

**Use of SLR observations to Sentinel-3A/B satellites allows for determination of station coordinates at level of 10 mm (best sites), geocenter coordinates at level of 6 mm, pole X,Y at level of 0.3 mas and Lod 0.06ms/day**

**Reference frame determination based of SLR measurements to Sentinels-3A/B can be delivered on SLR station reference frame**

**„SLR PPP” free network solution is possible based on SLR data and GPS orbits of LEO satellites at level of 10-mm**

Station coordinates shows the best consistency w.r.t. SLRF2014 while imposing **NNT/NNR** constraints with **parameter estimation and without network constraints and parameter estimation** („SLR-PPP”)

SLR station coordinates shows the best consistency w.r.t. SLRF2014 for **7 and 15 accumulated 1-day orbits**, whereas ERP and geocenter coordinates for 7 accumulated 1-day orbits



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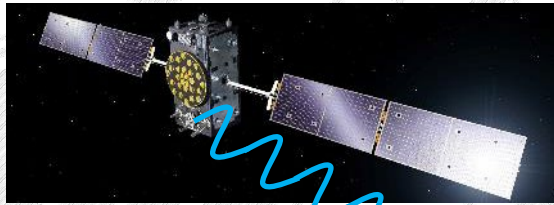
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BACK UP

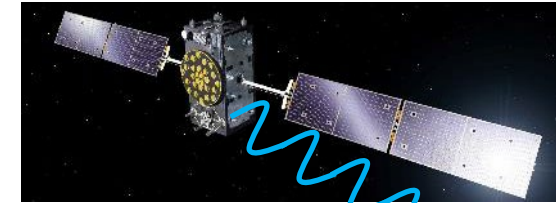
# The issue of the reference frame differences

## Test 3 no network constraints - SLR-PPP

### Test 1 with NNT/NNR constraints



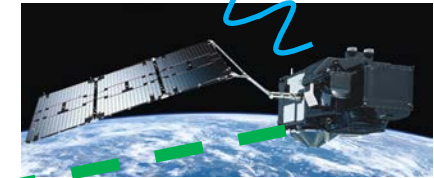
**GNSS – IGS14**  
integrated around  
Center-of-Figure (CoF)



**GNSS – IGS14**  
integrated around  
Center-of-Figure (CoF)



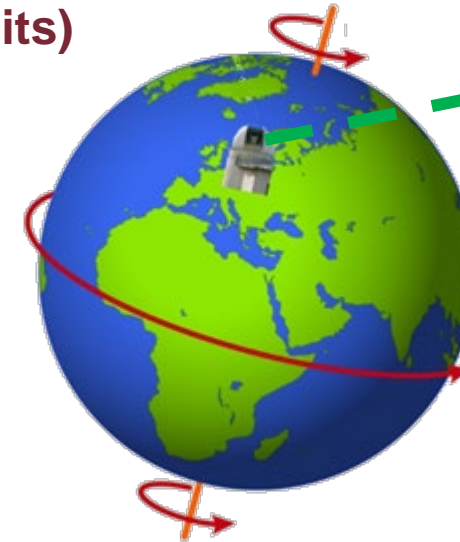
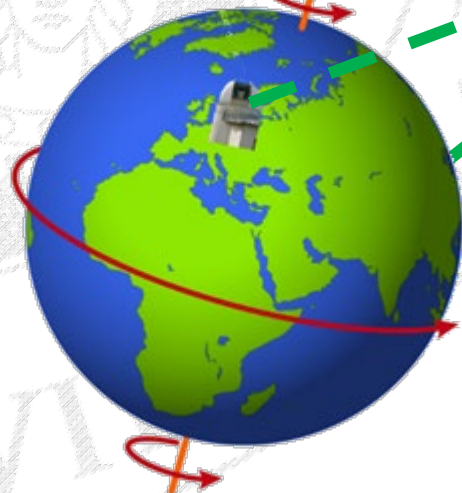
**SLR sites IGS14**  
(reference frame  
transferred through  
LEO orbits)



**LEO – IGS14,**  
reduced

**SLR sites in SLRF2014**  
(CoF by NNT/NNR)

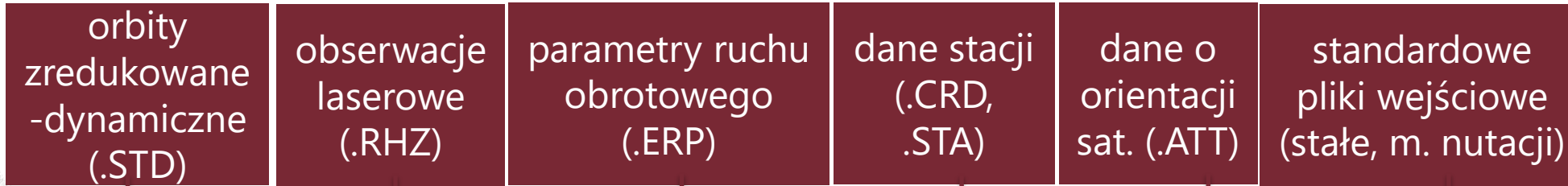
**LEO – IGS14,** but pseudo-stochastic orbit parameters are estimated → larger flexibility, close representation of the Earth's Center-of-Mass (CoM)



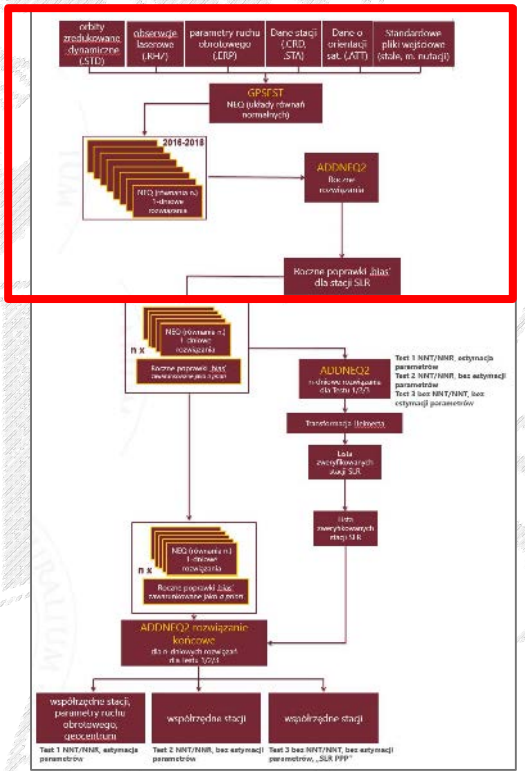
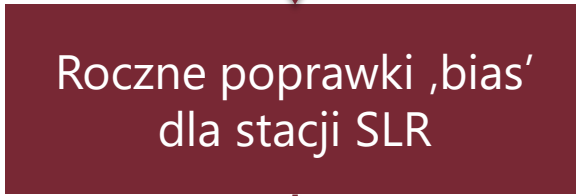
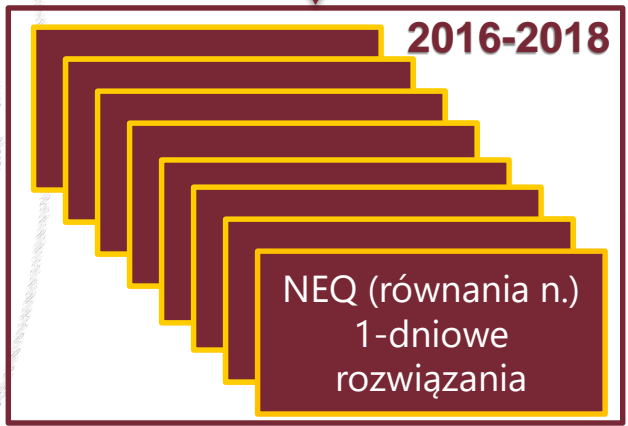
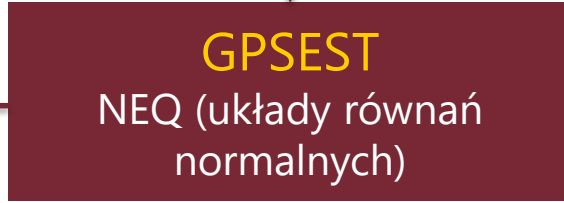
**In SLR-PPP (test3)**  
SLR station coord.  
are in IGS14

**CoM vector w.r.t. CoF represents geocenter motion,  
but to what extent IGS14 and SLRF2014 are consistent**

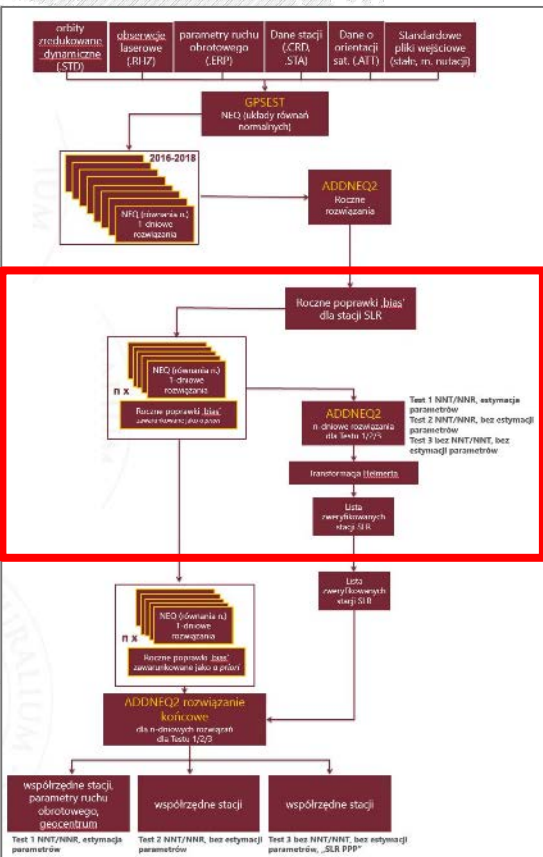
# Schemat obliczeń



Bernese GNSS Software modified 5.3 Version



**Bernese GNSS Software  
modified 5.3 Version**



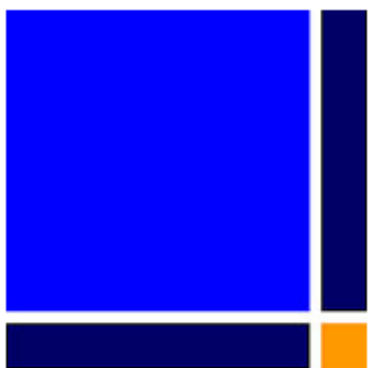
Roczne poprawki „bias” dla stacji SLR

**ADDNEQ2**  
n-dniowe rozwiązania dla Testu 1/2/3

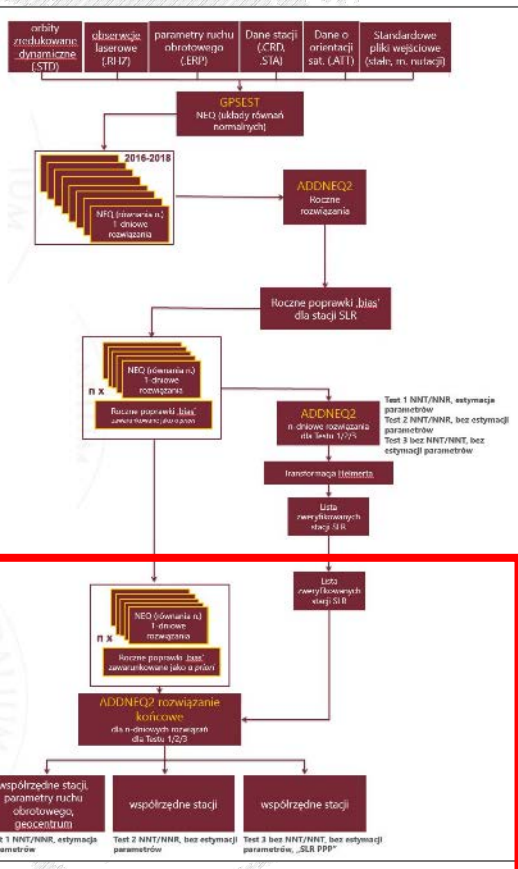
Transformacja Helmerta

Lista zweryfikowanych stacji SLR

Test 1 NNT/NNR, estymacja parametrów globalnych  
Test 2 NNT/NNR, bez estymacji parametrów globalnych  
Test 3 bez NNT/NNR, bez estymacji parametrów glob.



Bernese GNSS Software  
modified 5.3 Version



współrzędne stacji,  
parametry ruchu  
obrotowego,  
geocentrum

Test 1 NNT/NNR, estymacja parametrów glob.

współrzędne stacji

Test 2 NNT/NNR, bez estymacji parametrów glob.

współrzędne stacji

Test 3 bez NNT/NNR, bez estymacji parametrów glob., „SLR PPP”





**Table 2** SLR residuals (RMS and mean) of reduced-dynamic orbit solutions (identifier “N”) for days 001–365, 2007

Spacecraft	Solution ID	SLR residuals RMS (cm)	SLR residuals mean (cm)
GRACE A	N0	1.81	0.65
	N1 (5° × 5°)	1.81	0.65
	N4 (5° × 5°)	1.85	0.67
GRACE B	N0	2.02	0.85
	N1 (5° × 5°)	1.99	0.85
	N4 (5° × 5°)	1.95	0.83

Jäggi, A., Dach, R., Montenbruck, O., Hugentobler, U., Bock, H., Beutler, G., 2009. Phase center modeling for LEO GPS receiver antennas and its impact on precise orbit determination. *J Geod* 83(12):1145–1162



## SLR PPP

- zegary (jeden na stacji): bez estymacji
- niewielki wpływ troposfery
- biasy (opóźnienia sprzętowe): jeden na mierzoną odległość (błąd wyznaczenia centrum optycznego, błędy kalibracji, opóźnienie syg. w kablach), ale stabilne i wyznaczane w długich okresach (1 na rok)

## GNSS PPP

- zegary (osobny na stacji i osobny na sat.): estymacja dodatkowego parametru
- duży wpływ troposfery
- biasy: niestabilne, estymacja 1 na dobę (różnice między systemami, między częstotliwościami, między satelitami, biasy fazy i kodu)

## TOP SITES

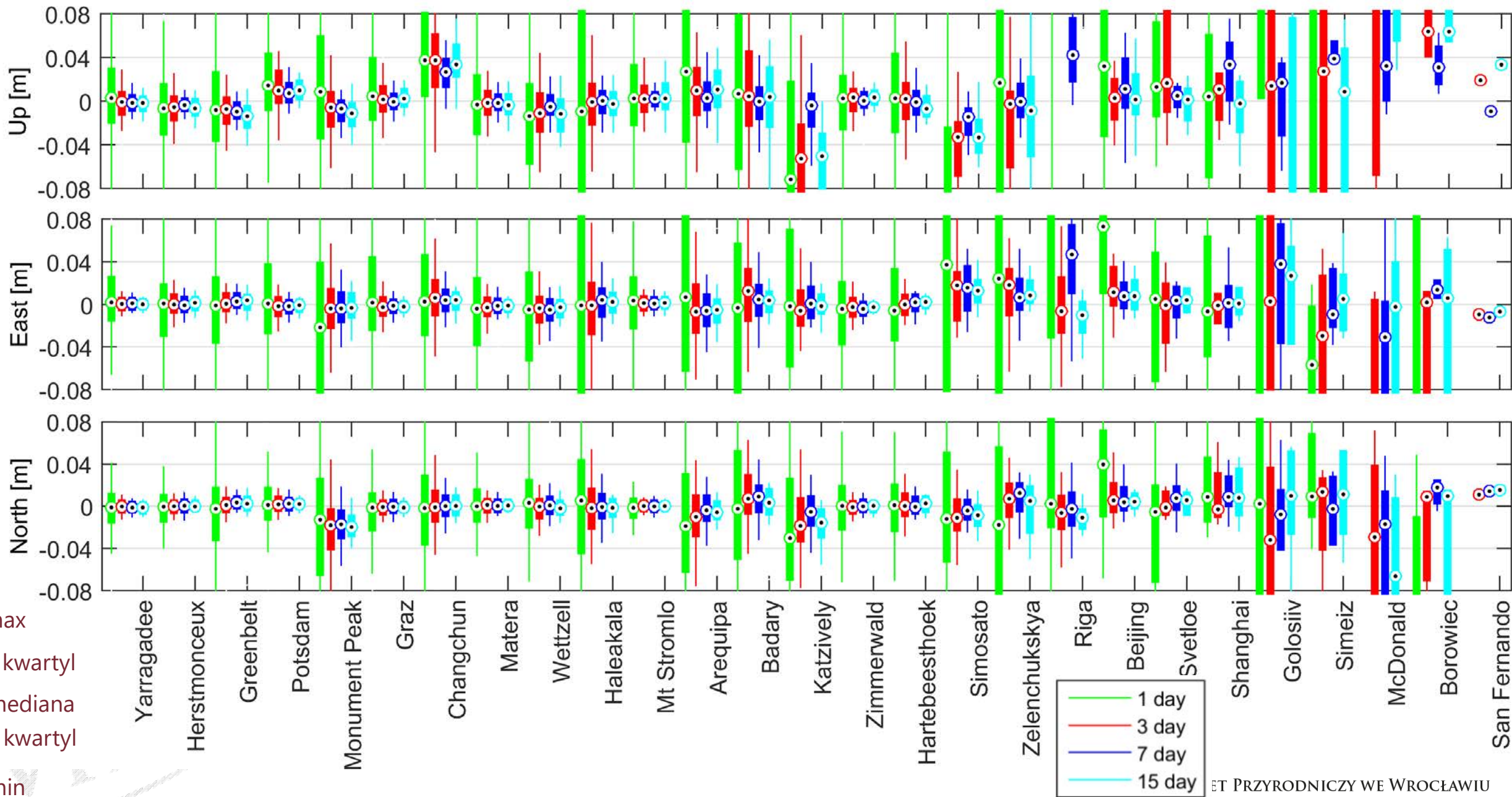


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No. of sites	Solution	N [mm]		E [mm]		Up [mm]	
		median	IQR	median	IQR	median	IQR
All sites	LAG	-0.9	12.7	0.5	11.1	-0.8	24.6
	Sent	0.0	11.7	0.2	13.4	-0.8	16.3
	LAG+Sent	-1.0	12.4	0.3	11.4	-1.3	26.3
Top sites	LAG	-0.1	5.3	0.0	5.0	-0.4	12.5
	Sent	0.5	7.8	-0.4	9.1	-1.6	11.9
	LAG+Sent	-0.2	5.2	-0.1	5.2	-0.7	12.3

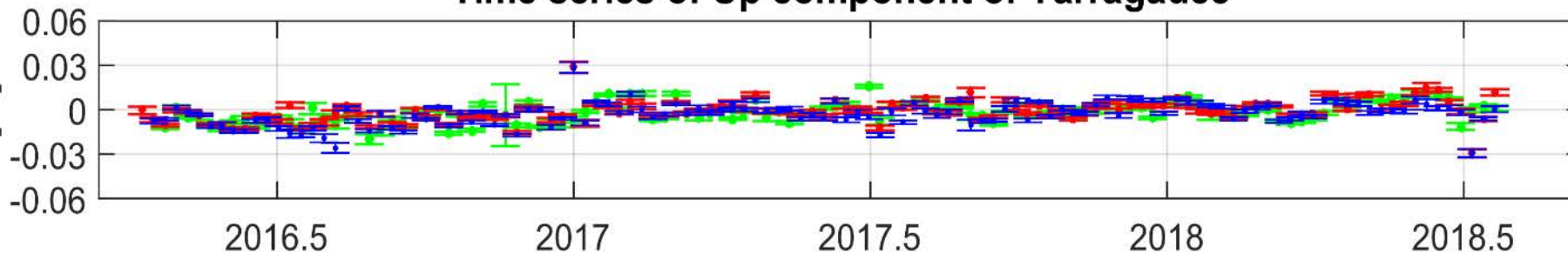
**Yarragadee, Herstmonceux, Greenbelt, Graz, Potsdam, Matera, Wettzell,  
Haleakala, Mt Stromlo, Hartebeesthoek, Zimmerwald**

# Testy rozwiązań – różnej liczby $n$ jednodniowych orbit w rozwiązaniach

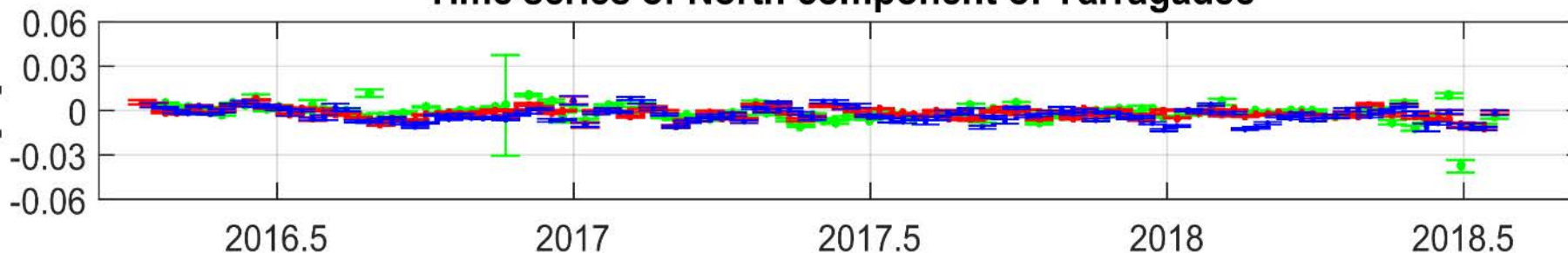


# Testy warunkowania – współrzędne stacji 7-dniowe rozwiązanie – Sentinel-3A/B

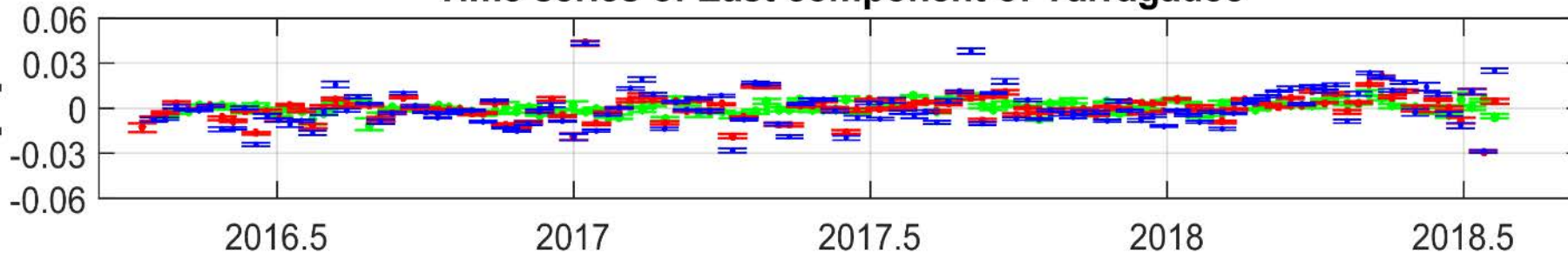
Time series of Up component of Yarragadee



Time series of North component of Yarragadee



Time series of East component of Yarragadee



- NNT/NNR, estymacja parametrów glob.
- NNT/NNR, bez estymacji parametrów glob.
- bez NNT/NNR, bez estymacji parametrów glob.

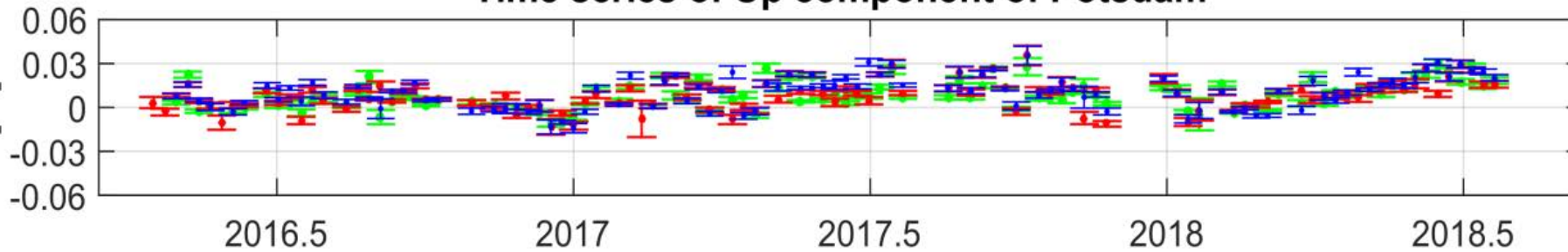
Powtarzalność stacji dla poszczególnych składowych na poziomie od 5-9 mm

Zbliżone wyniki również dla testu bez warunkowania sieci (Test 3)

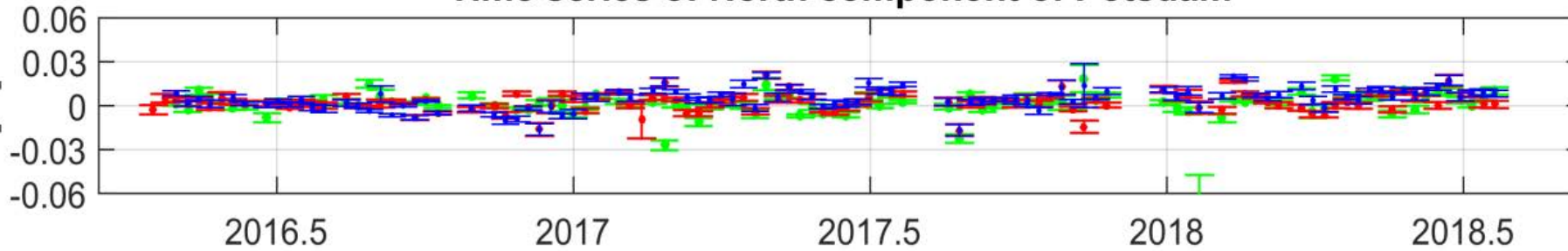
Test3 można nazwać „**SLR-PPP**”, bo zależny wyłącznie od jakości orbit oraz jakości i ilość obs. SLR

# Testy warunkowania – współrzędne stacji 7-dniowe rozwiązanie – Sentinel-3A/B

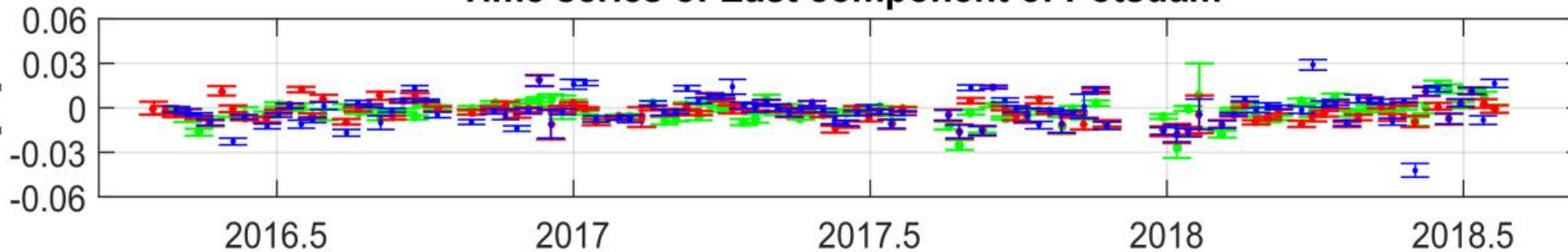
Time series of Up component of Potsdam



Time series of North component of Potsdam



Time series of East component of Potsdam



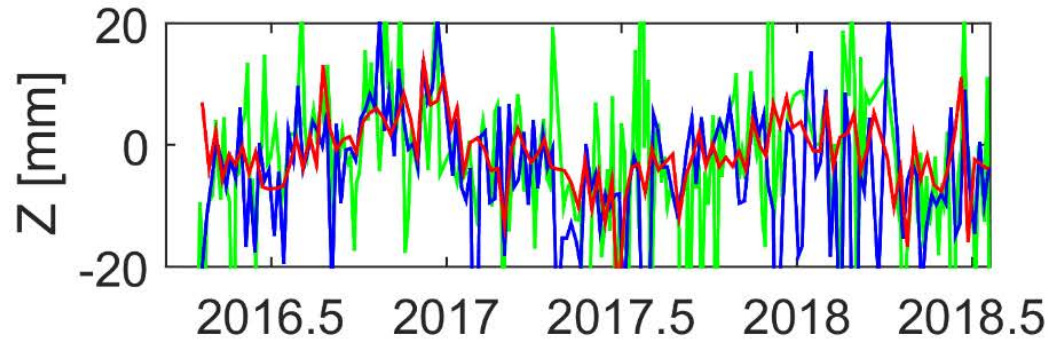
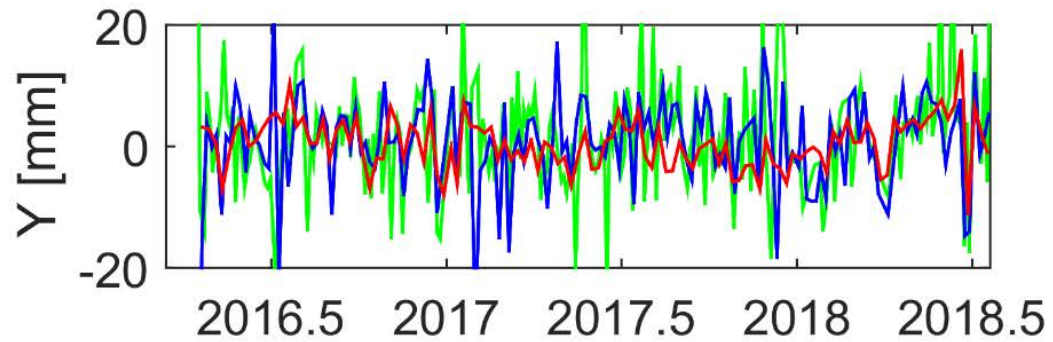
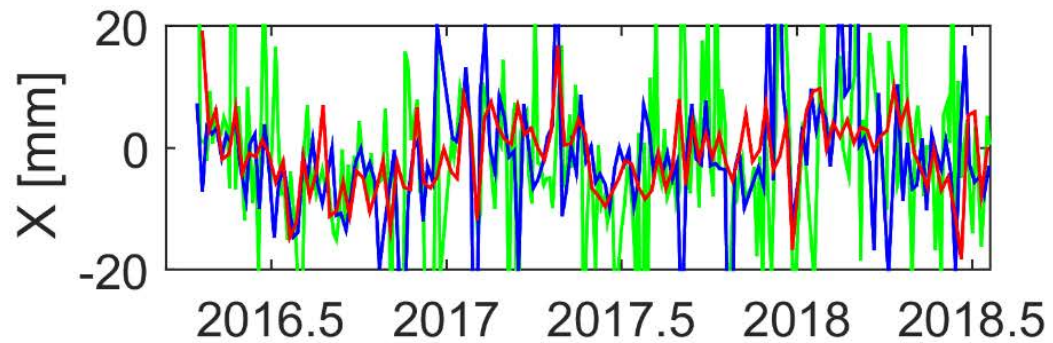
- NNT/NNR, estymacja parametrów glob.
- NNT/NNR, bez estymacji parametrów glob.
- bez NNT/NNR, bez estymacji parametrów glob.

Powtarzalność stacji dla poszczególnych składowych na poziomie od 7-14 mm

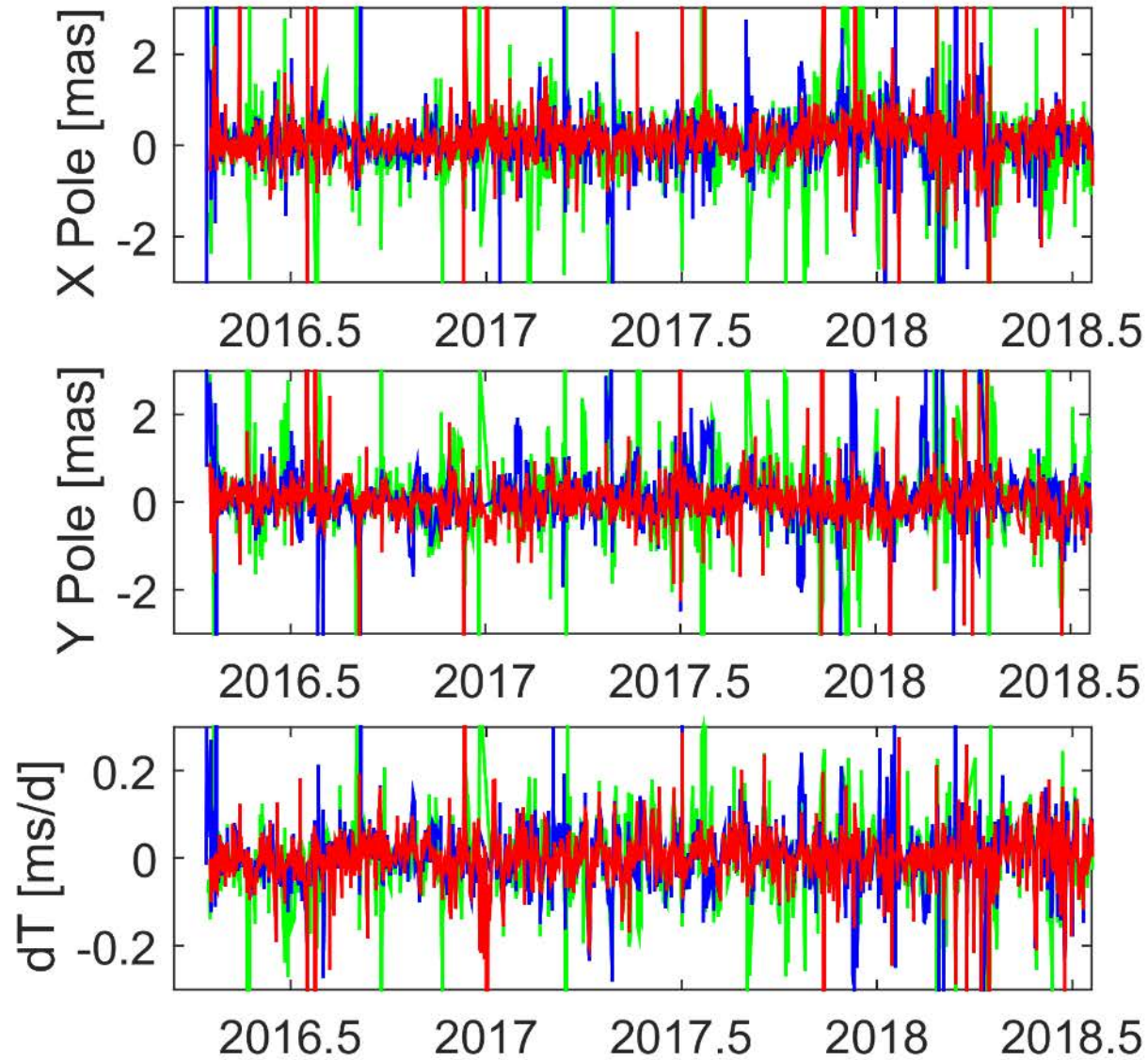
Zbliżone wyniki również dla testu bez warunkowania sieci (Test 3)

1-cm dokładność wyznaczenia współrzędnych

# Testy rozwiązań – wyznaczenie współrzędnych geocentrum– Sentinel-3A/B



# Testy rozwiązań – wyznaczenie parametrów ERP – Sentinel-3A/B

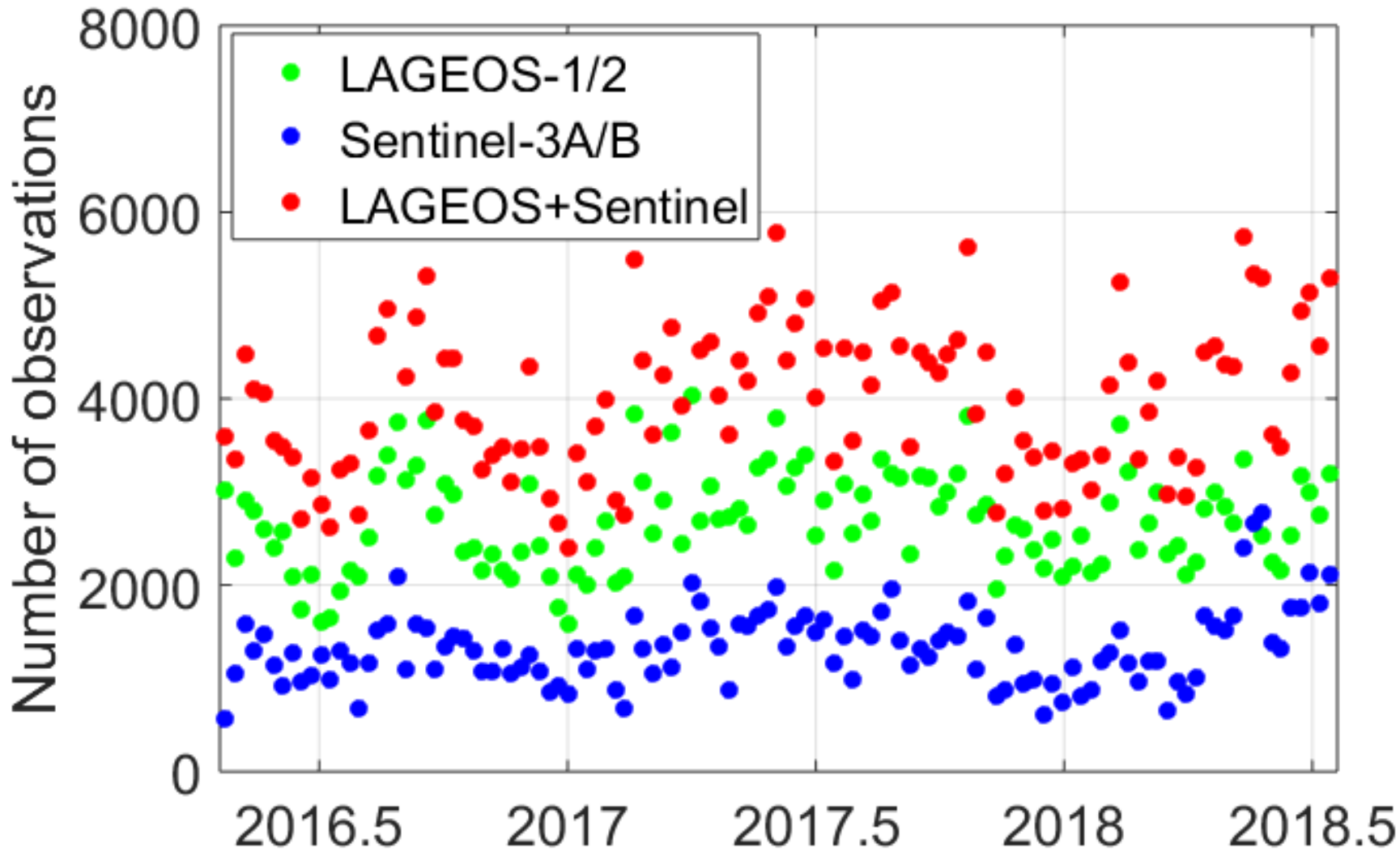


Porównanie względem produktów C04 (dane IER)





# Statistics



7-dniowe orbity  
Rozwiązanie test 1  
(NNT/NNR, estymacja parametrów glob.)

345,692 NP dla LAGEOS  
157,213 NP dla Sentinel 3  
502,905 NP rozwiązania łącznego

# No. of obs. increase

