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OF ENVIRONMENTAL  
AND LIFE SCIENCES

# High-rate GNSS in seismology

**Correction of multipath effect for precise point positioning  
high-rate GNSS data processing in seismic phenomena analysis**

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INCREaSE - GEOworkshop

Wrocław, 28.03.2019 r.

# Outline

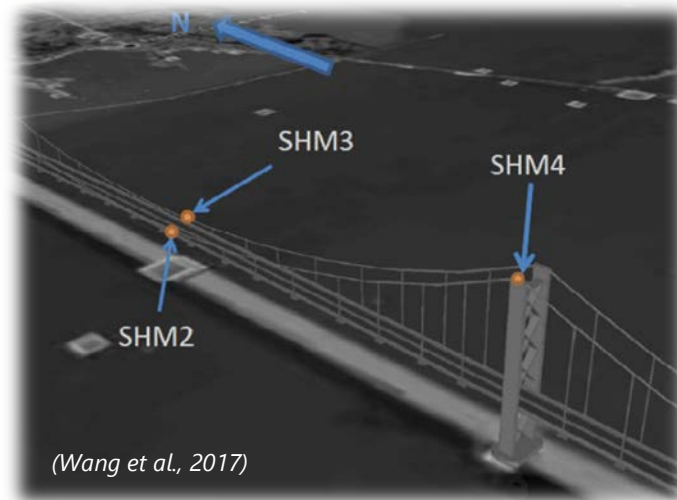
- Motivation
- HR-GNSS in seismology
- Multipath error mitigation
  - Position Domain Sidereal Filtering
  - Multipath Hemispherical Map
  - Digital Filtering
- The application of HR-GNSS in mining tremor analysis

# Motivation

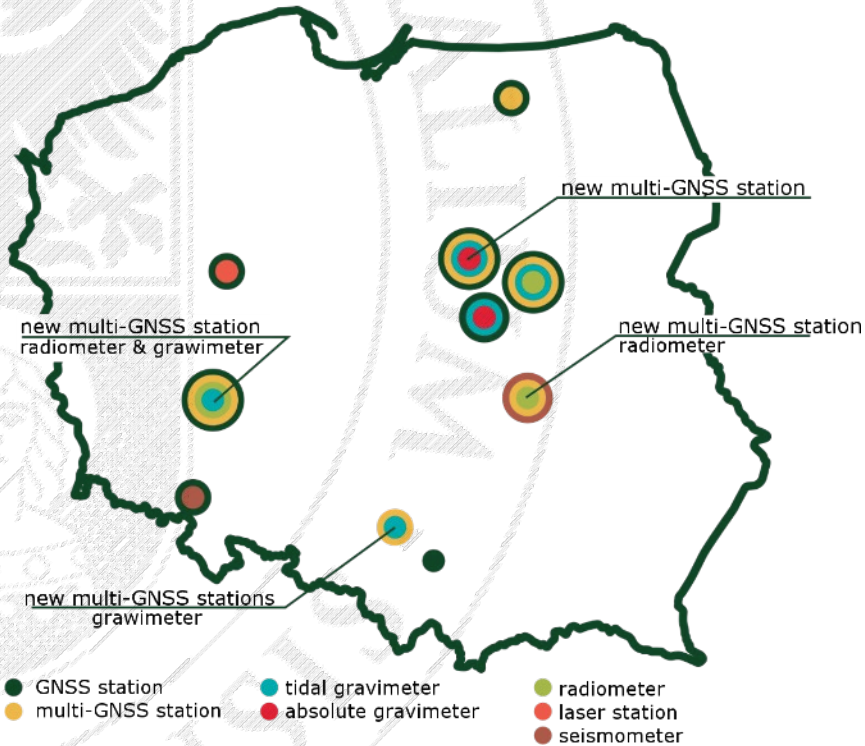
## HR-GNSS

- high precision
- information on GNSS station location changes in small time intervals

- earthquake analysis, including early warning systems
- structural health monitoring, eg. bridges



HR-GNSS network in Poland dedicated to mining deformation analysis with particular emphasis on the area of the Upper Silesian Coal Basin



USCB mining damages



Co-located geophysical and geodetic infrastructure enables to integrate the data.

# HR-GNSS in seismology

## Differential Positioning (DP)

- in case of earthquakes – the position of reference station may be changed

## Precise Point Positioning (PPP)

- empirical analysis showed that HR-PPP in short period of time reaches millimeter precision (Hefty and Gerhátová, 2012; Xu et al., 2013), which is a better result than traditional PPP

## Variometric Approach

*(Colosimo et al., 2011; Benedetti et al., 2016)*

- Variometric Approach for Displacements Analysis Stand-alone Engine (VADASE)
- the epoch-by epoch displacements (equivalent to inter-epoch mean velocities) are estimated in a global reference frame using the phase observations from the satellites in view in two consecutive epochs
- few-minutes long time series, centimeter accuracy

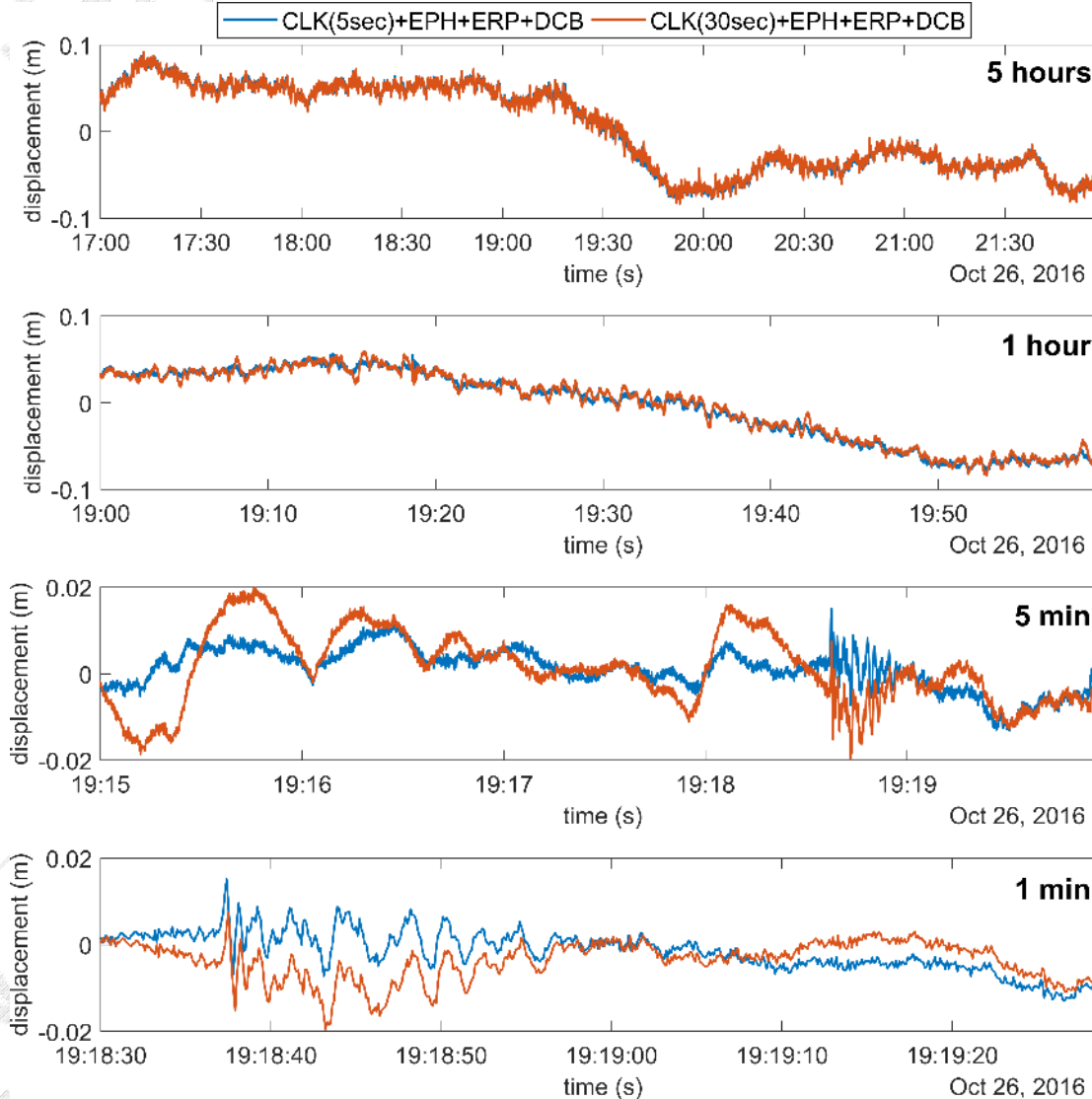
# HR-PPP – the influence of CODE products on time series

*Clock data*

RTKlib 2.4.3

Kinematic PPP

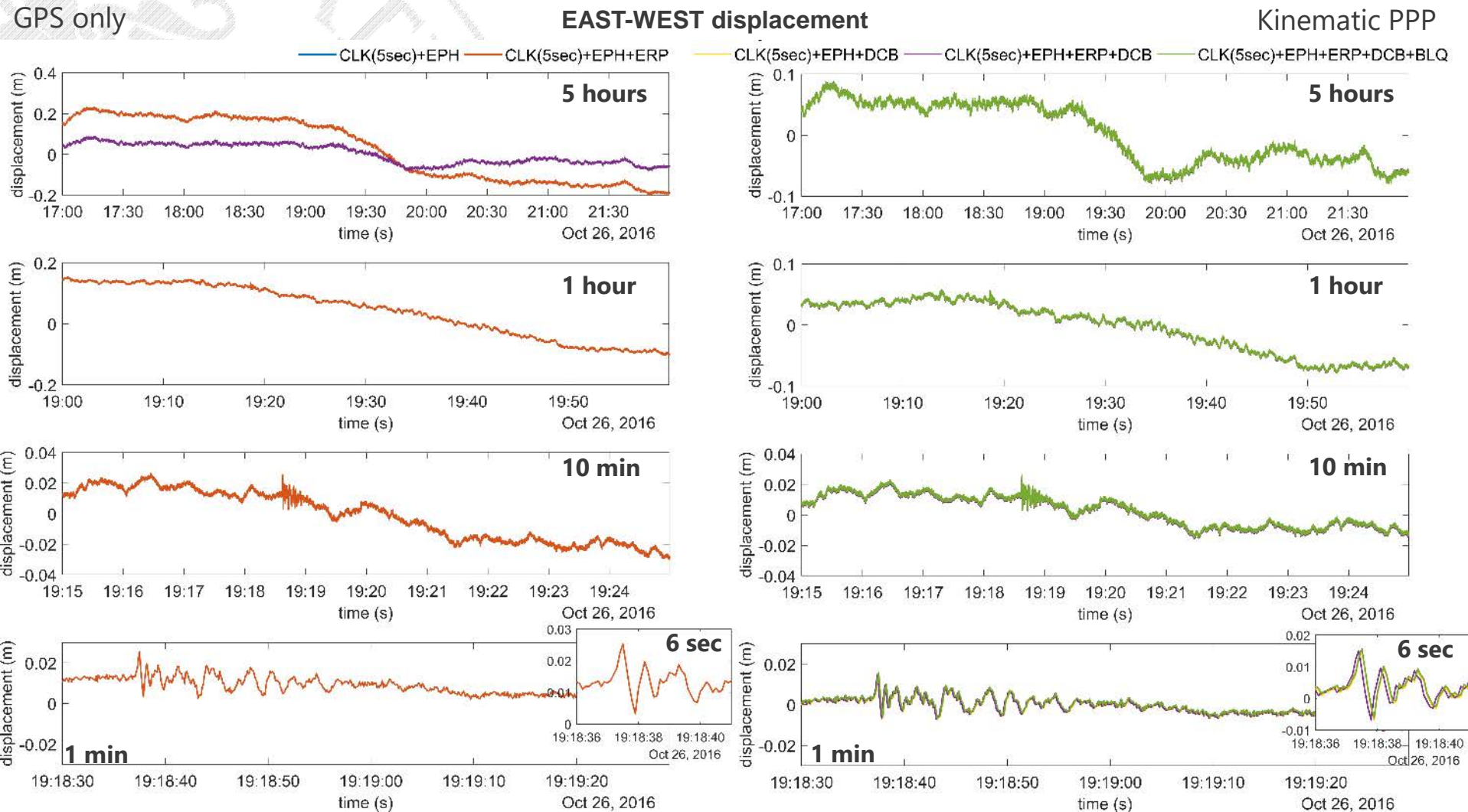
**EAST-WEST displacement**



GPS: AMAT (10Hz);  
EQ Norcia 2016-10-26  
19:18:08 UTC, Mw 6.6

# HR-GNSS – the influence of CODE products on time series

RTKlib 2.4.3  
Kinematic PPP



RMS & correlation coefficients → ERP, BLQ – no influence in HR-PPP within short periods of time

GPS: AMAT (10Hz);  
EQ Norcia 2016-10-26  
19:18:08 UTC, Mw 6.6

# Observation errors in HR-GNSS

## HR-GNSS

position analysis in subsequent epochs

short (several-minute) time series analysis

large influence of systematic errors

errors resulting from  
satellite geometry

errors resulting from  
geophysical effects

errors resulting from  
clock-drift

random errors

higher-order ionospheric  
errors

multipath error

mostly eliminated by  
corrections and models

should be taken  
into account

*eg. using interpolated clock*

*eg. sidereal filtering  
multipath maps*

*in case of*

- high ionospheric activity*
- large earthquakes*



# Multipath error reduction in HR-GNSS

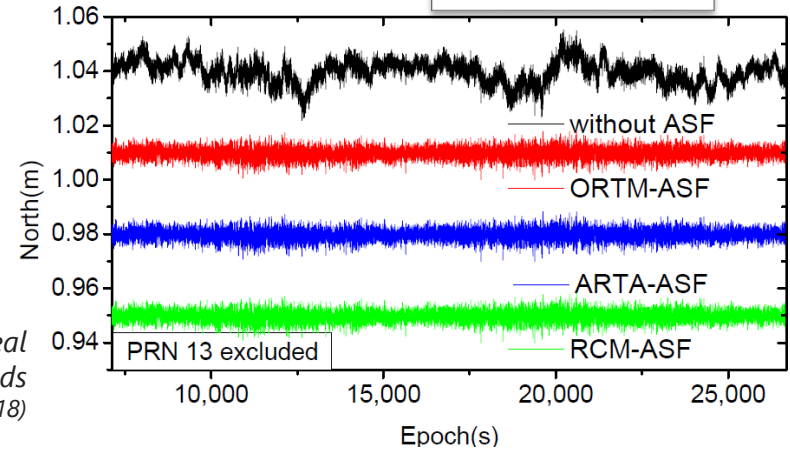
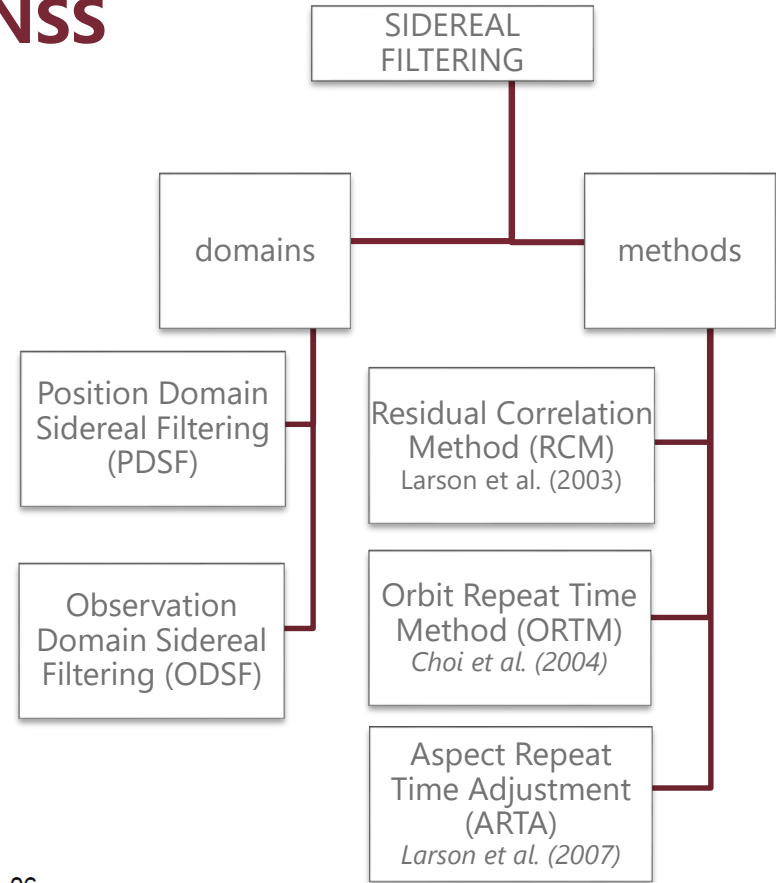
## Methods:

- **Sidereal filtering**

The model is built of coordinates or observation residuals from of the previous day(s). Then the correction of the data of the subsequent day(s) is applied by subtracting the corresponding correction value for each epoch considering the sidereal day shift.

(eg. Bock et al., 2000; Choi et al., 2004; Emore et al., 2007)

- **Multipath hemispherical maps**
- **Digital filtering**



Displacement time series influenced by different sidereal filtering methods (Wang et al., 2018)

# Multipath error reduction in HR-GNSS

## Methods:

- **Sidereal filtering**
- **Multipath hemispherical maps**

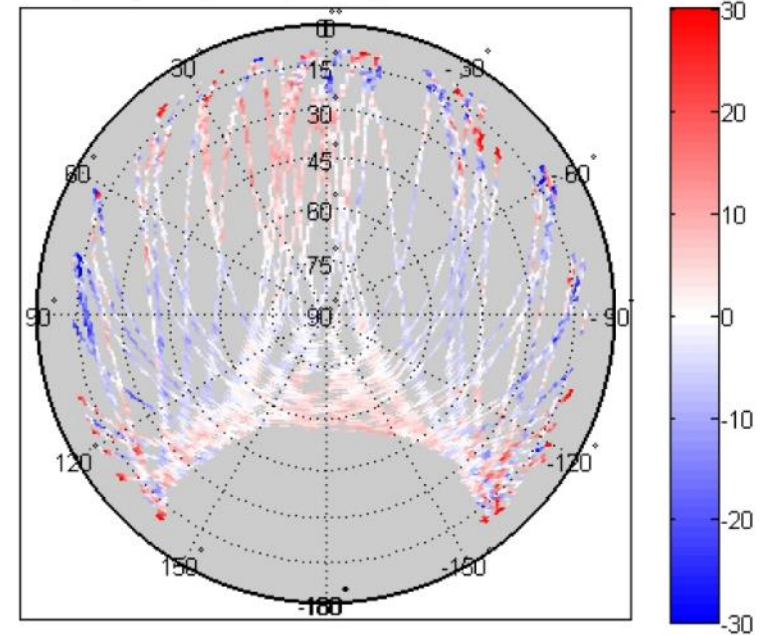
*The model is built with carrier-phase residuals in a grid with fixed density for the GNSS receiver located in a specific location. Then the observations in each cell are corrected.*

*(eg. Moore et al., 2013; Fuhrmann et al., 2014; Dong et al., 2015)*

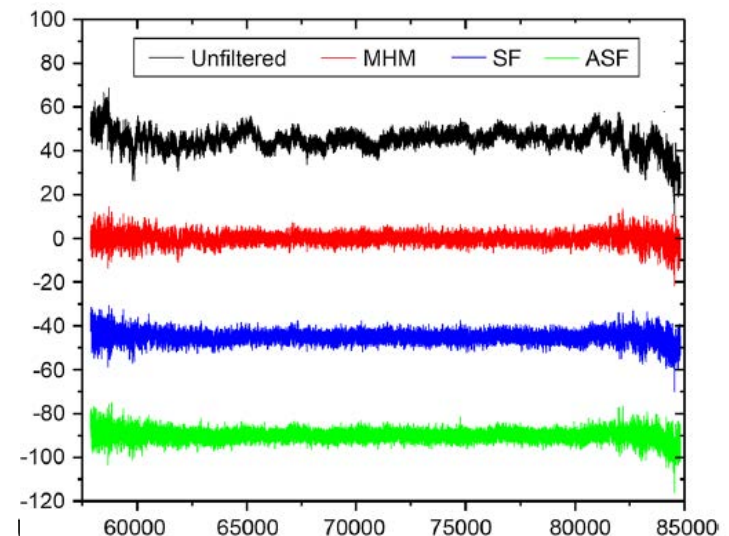
- **Digital filtering**

*(Kamatham et al., 2013)*

Single day multipath map PERT, phase residuals in mm



Multipath map for PERT station  
(Huisman et al., 2009)



PRN 09 L1-residuals  
(Dong et al., 2015)

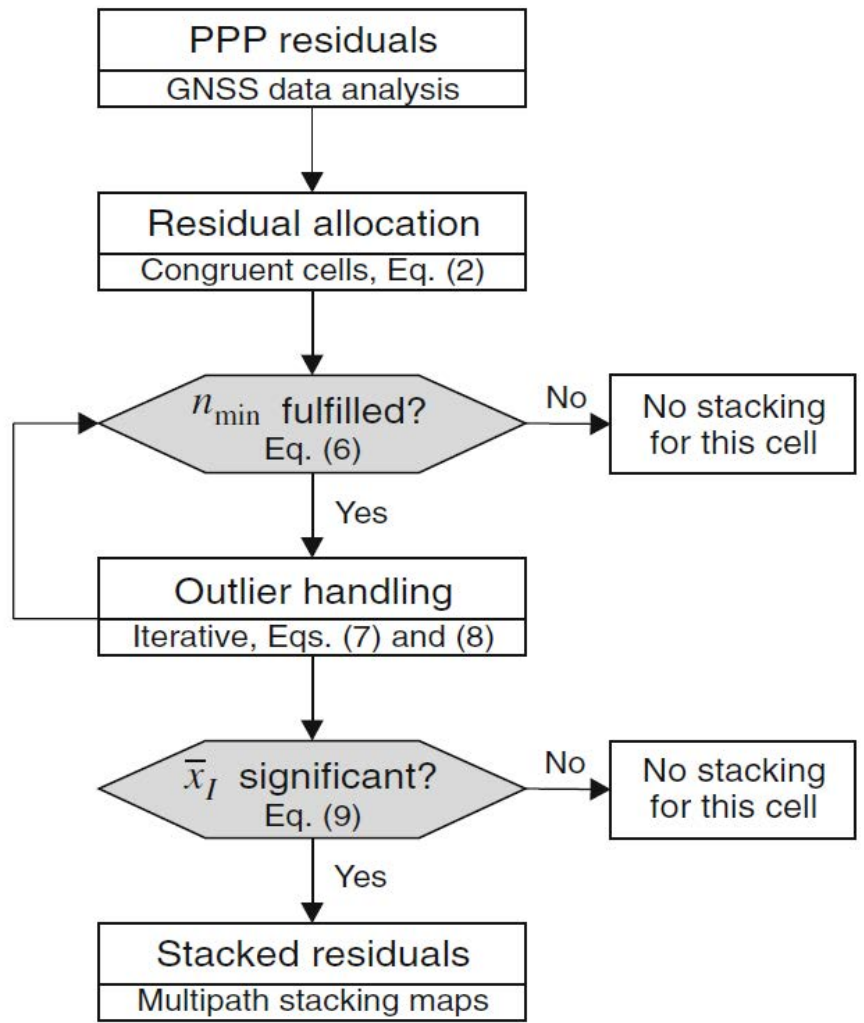


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Seismic phenomena in the light of high-rate GPS  
Precise Point Positioning results  
*MULTIPATH MAPS*

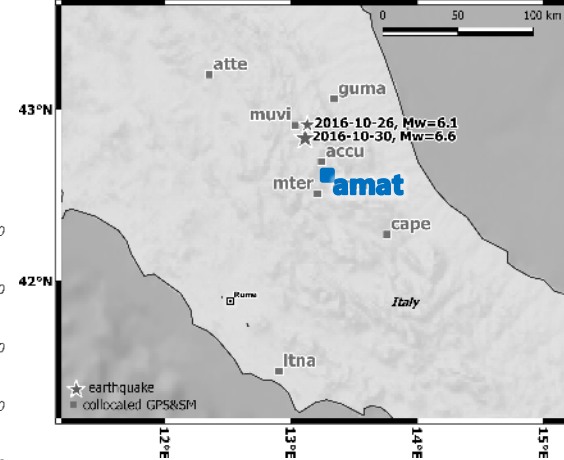
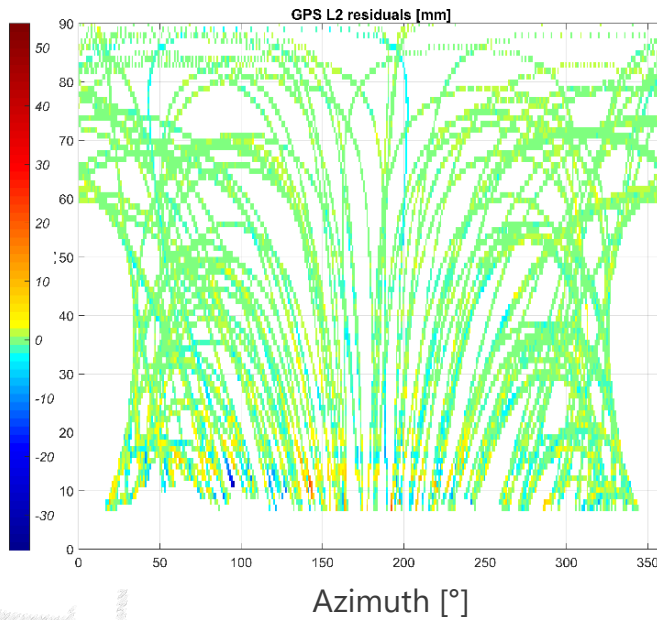
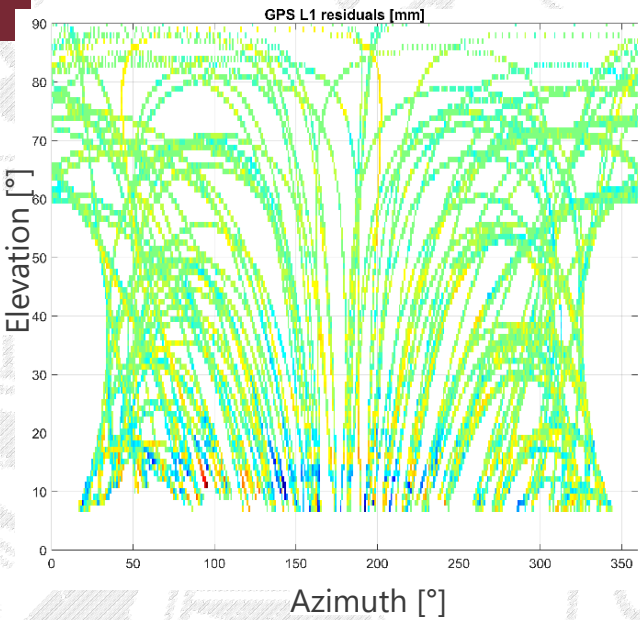
# Multipath map generation scheme

- ✓ 30-days 30-sec observations
- ✓ processed with CSRS-PPP v2.21.0
  - static mode
  - GPS (+GLONASS)
  - IGS Final
  - elevation: 7.5°
- ✓ carrier-phase observations
- ✓ **maps obtained separately for L1-L2 frequencies**



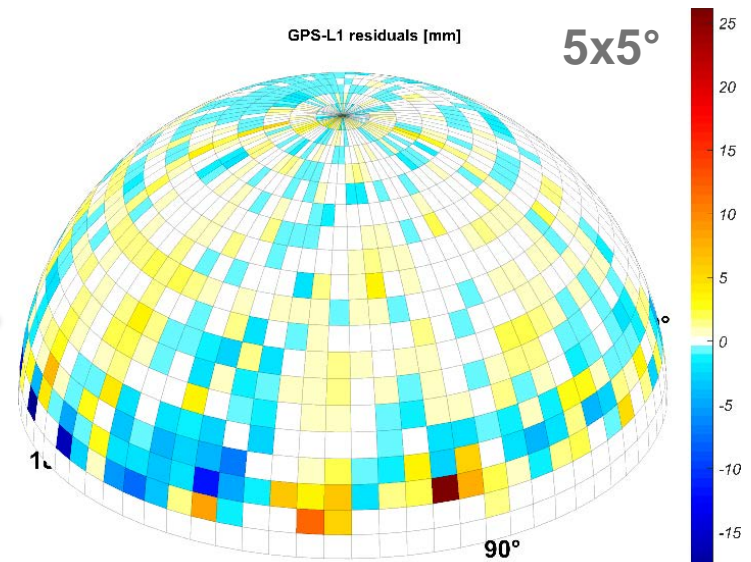
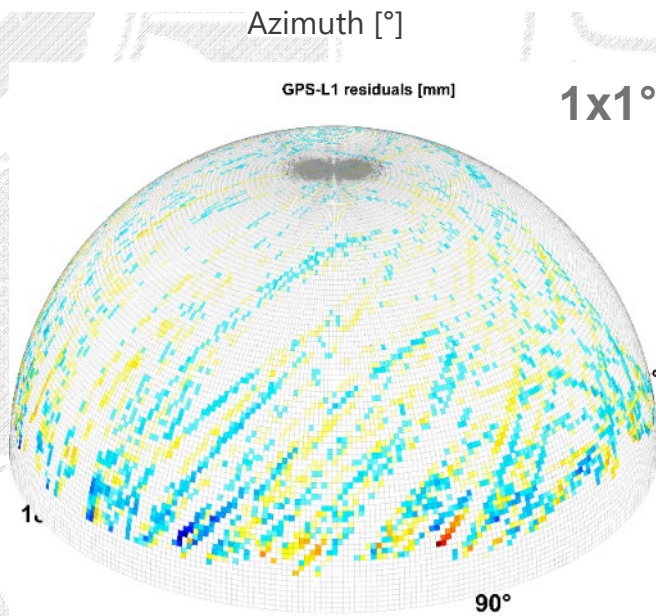
Flowchart of the proposed stacking approach using congruent cells  
(Fuhrmann et al., 2014)

# Multipath 1x1° map for AMAT station



GPS: AMAT (10Hz);  
EQ Norcia 2016-10-26  
19:18:08 UTC, Mw 6.6

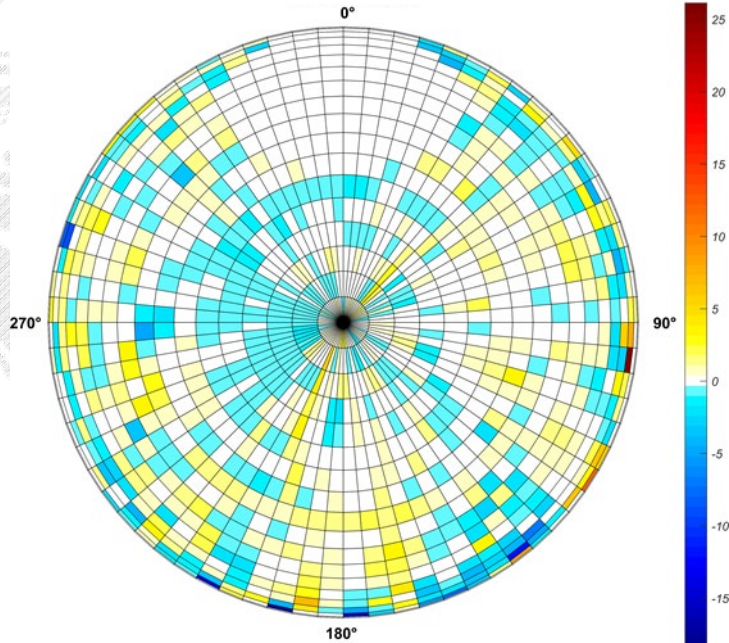
antenna: LEIAR25.R4 LEIT  
system: GPS



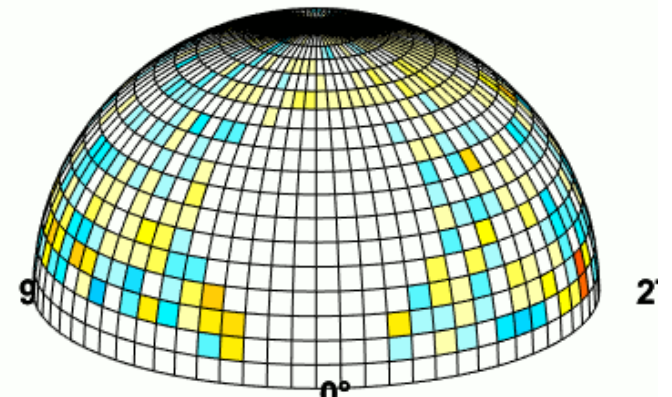
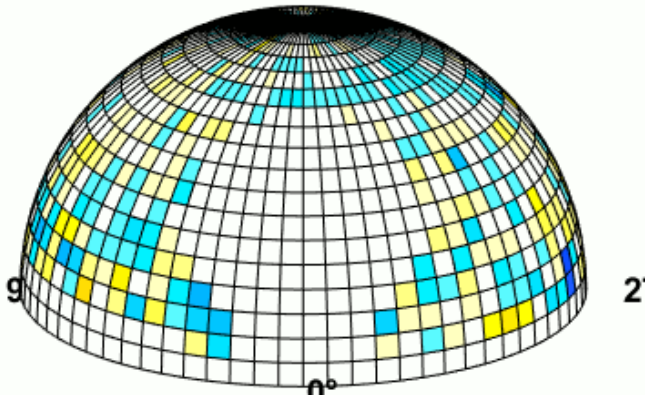
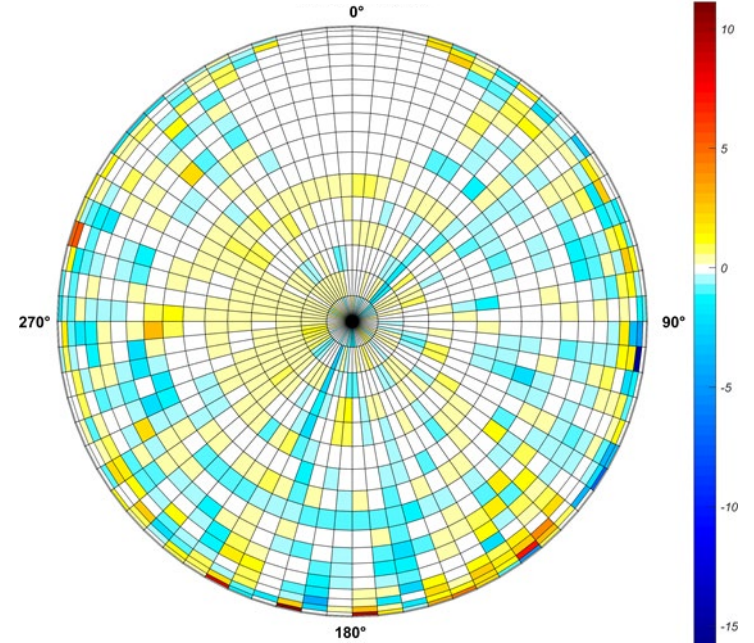
# PCV antenna model corrected with multipath map

*AMAT station*

GPS L1 PCV+MP [mm]

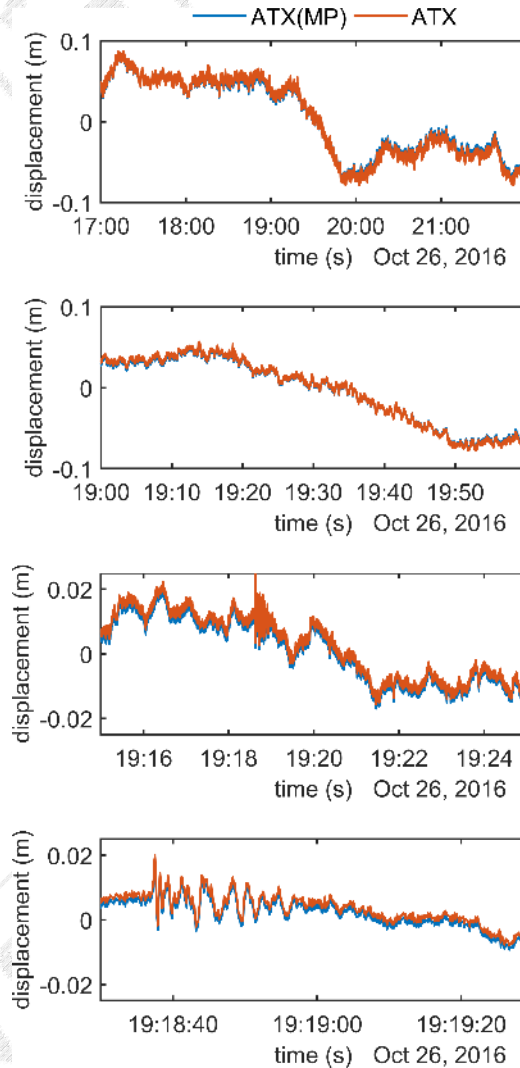


GPS L2 PCV+MP [mm]

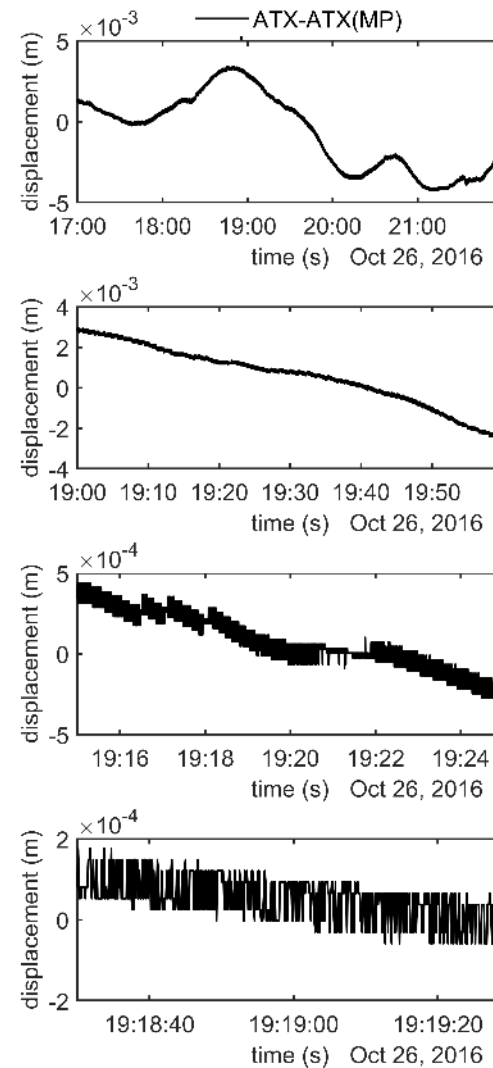


# Result

### EW displacement



### EW difference





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Seismic phenomena in the light of high-rate GPS  
Precise Point Positioning results  
*POSITION DOMAIN SIDEREAL FILTERING*



# Position Domain Sidereal Filter generation scheme

$$\begin{bmatrix} X_{k_1}^{est} \\ Y_{k_1}^{est} \\ Z_{k_1}^{est} \end{bmatrix} - \begin{bmatrix} X \\ Y \\ Z \end{bmatrix} = \begin{bmatrix} \delta X_{k_1} \\ \delta Y_{k_1} \\ \delta Z_{k_1} \end{bmatrix} \xrightarrow{\text{low-pass filter}} \begin{bmatrix} \delta X_{k_1} \\ \delta Y_{k_1} \\ \delta Z_{k_1} \end{bmatrix}_F$$

$$\begin{bmatrix} X_{k_2} \\ Y_{k_2} \\ Z_{k_2} \end{bmatrix}_{corr} = \begin{bmatrix} X_{k_2}^{est} \\ Y_{k_2}^{est} \\ Z_{k_2}^{est} \end{bmatrix} - \begin{bmatrix} \delta X_{k_1} \\ \delta Y_{k_1} \\ \delta Z_{k_1} \end{bmatrix}_F$$



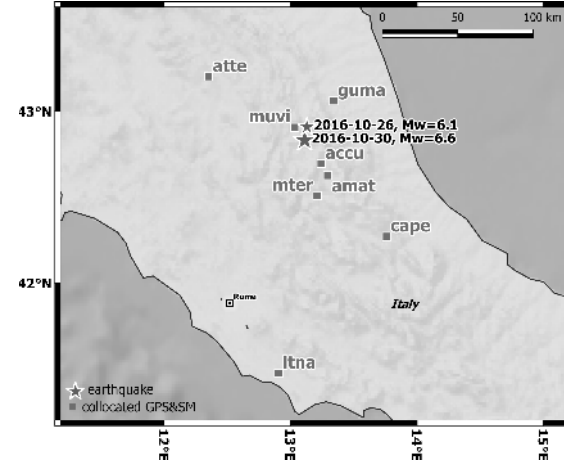
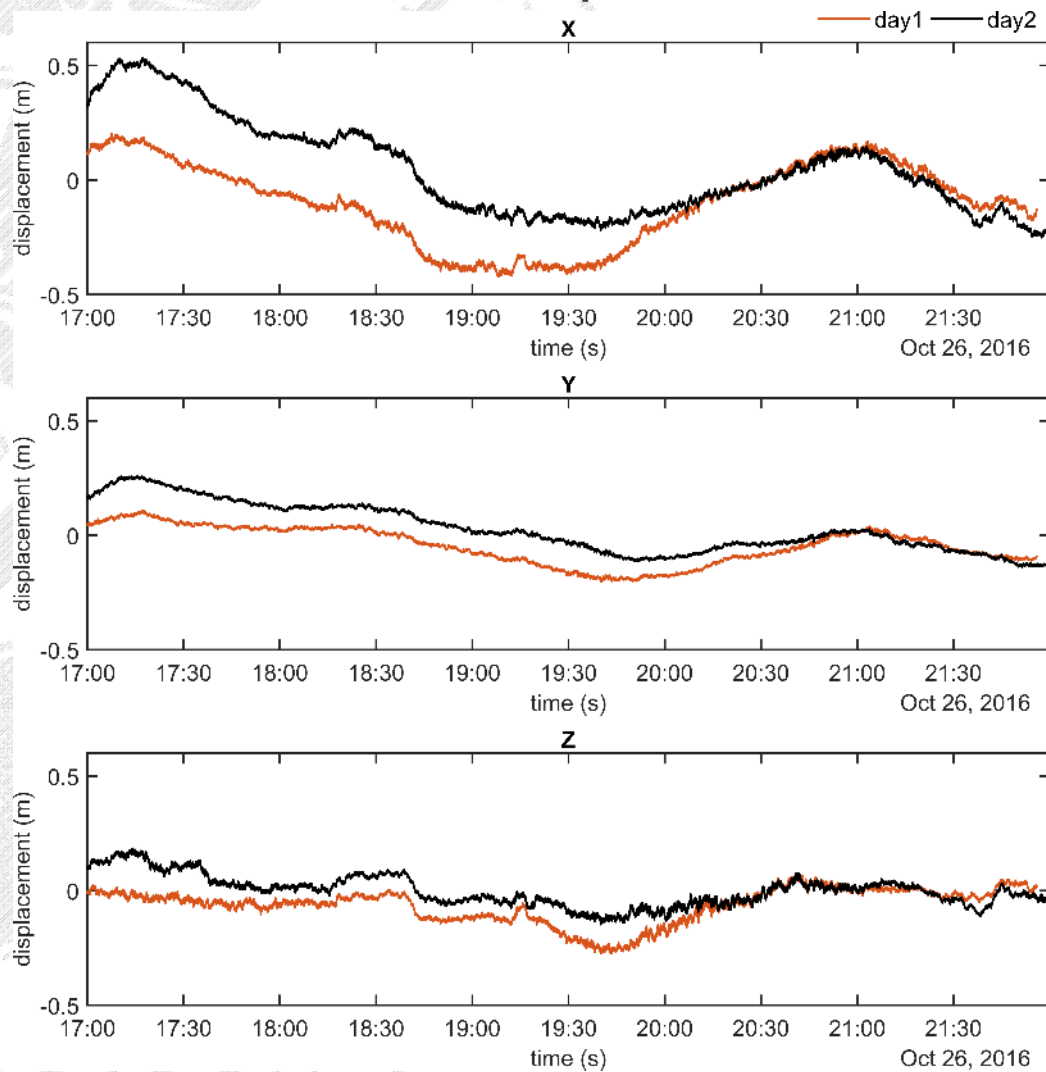
shifted by the satellite repeat period

$$t_{k_2} = t_{k_1} + t_{repeat}$$

$$t_{repeat} = 86\,155\,s = 23\,h\,55\,min\,4\,s$$

# Example

## Nonfiltered displacements



GPS: AMAT (10Hz);  
EQ Norcia 2016-10-26  
19:18:08 UTC, Mw 6.6

RTKlib 2.4.3  
CLK(5sec)+EPH+ERP+DCB

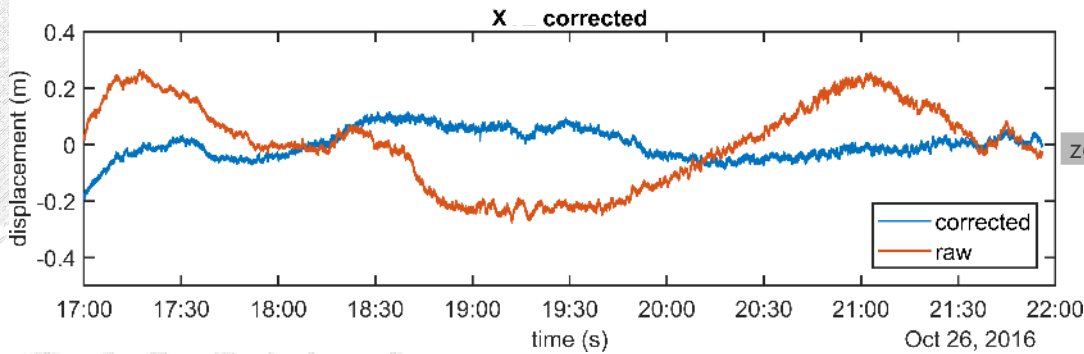
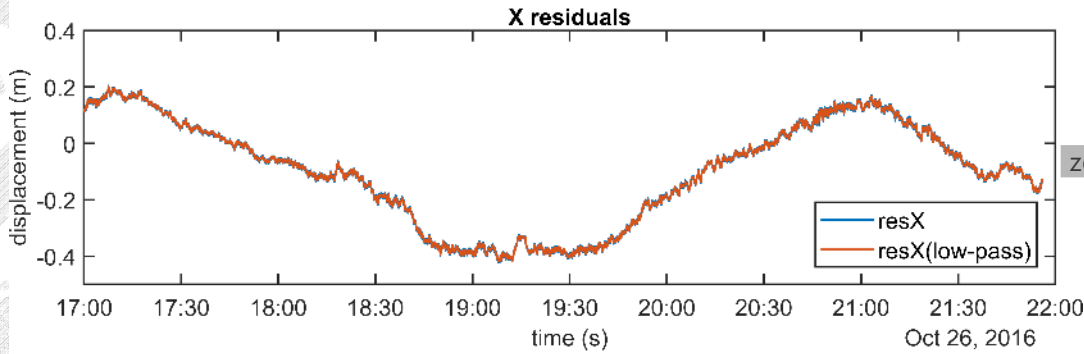
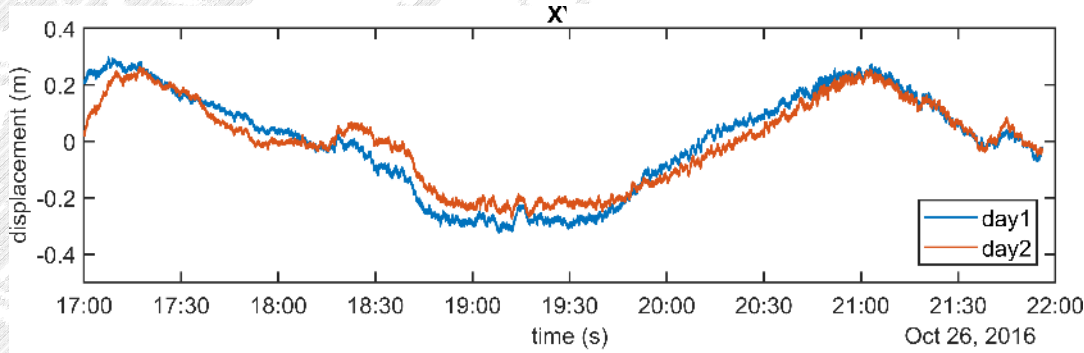
The data from DAY 1 is shifted by the sidereal day, for clarity

# Example

GPS: AMAT (10Hz);  
EQ Norcia 2016-10-26  
19:18:08 UTC, Mw 6.6

RTKlib 2.4.3  
CLK(5sec)+EPH+ERP+DCB

## Mechanism of PDSF

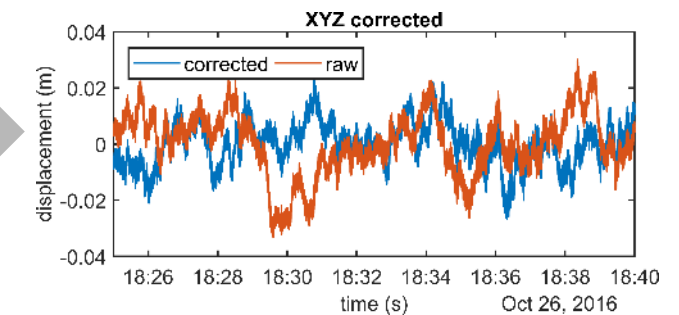
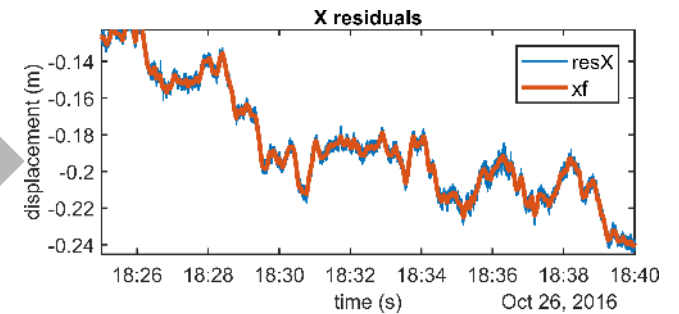


zoom

zoom

## RMS GPS

	5 hours		15 min	
	raw	corrected	raw	corrected
'X'	0.148	0.051	0.011	0.008
'Y'	0.051	0.024	0.006	0.003
'Z'	0.058	0.034	0.008	0.006

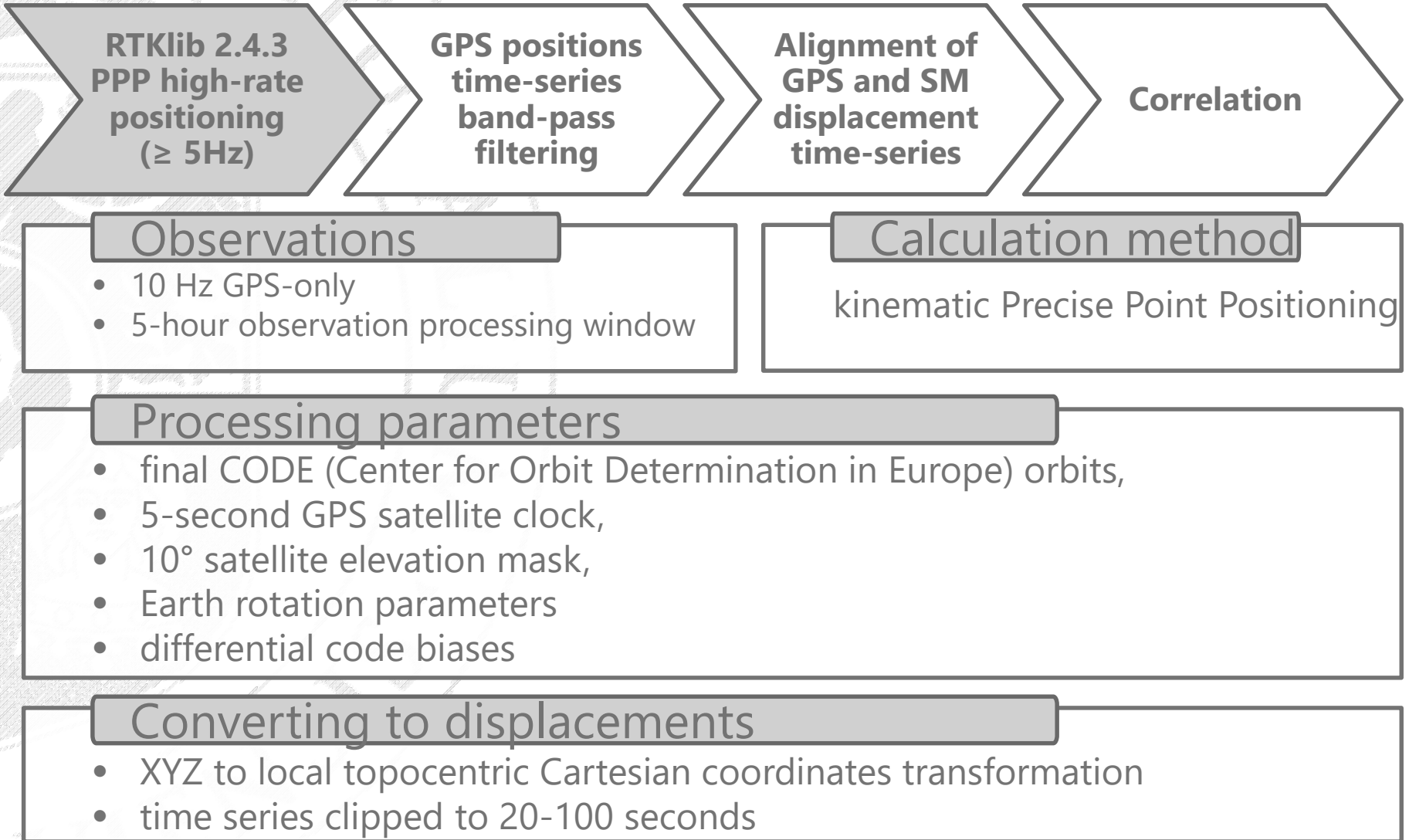




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Precise Point Positioning results  
*DIGITAL FILTERING*

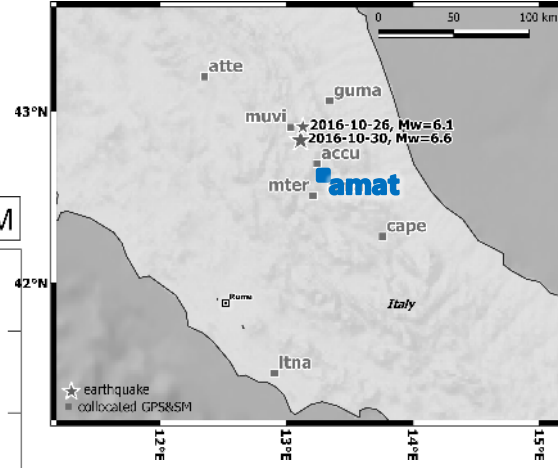
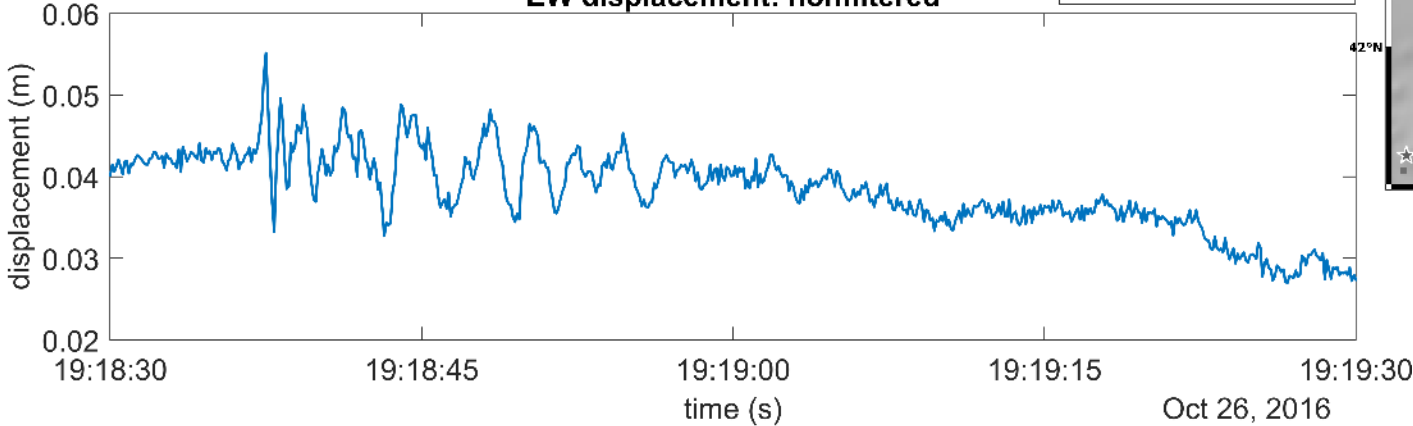
# HR-GNSS processing schema



# HR-GNSS vs SM -example

EW displacement: nonfiltered

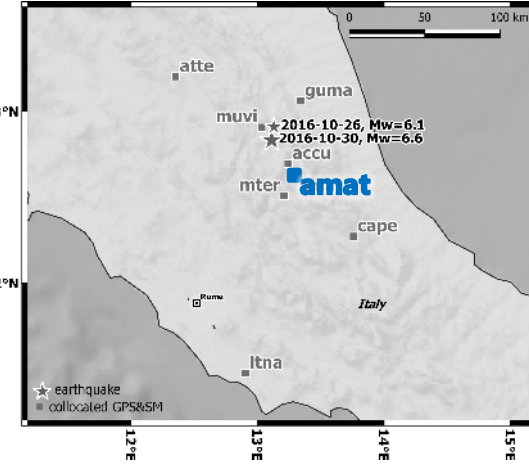
— GNSS — SM



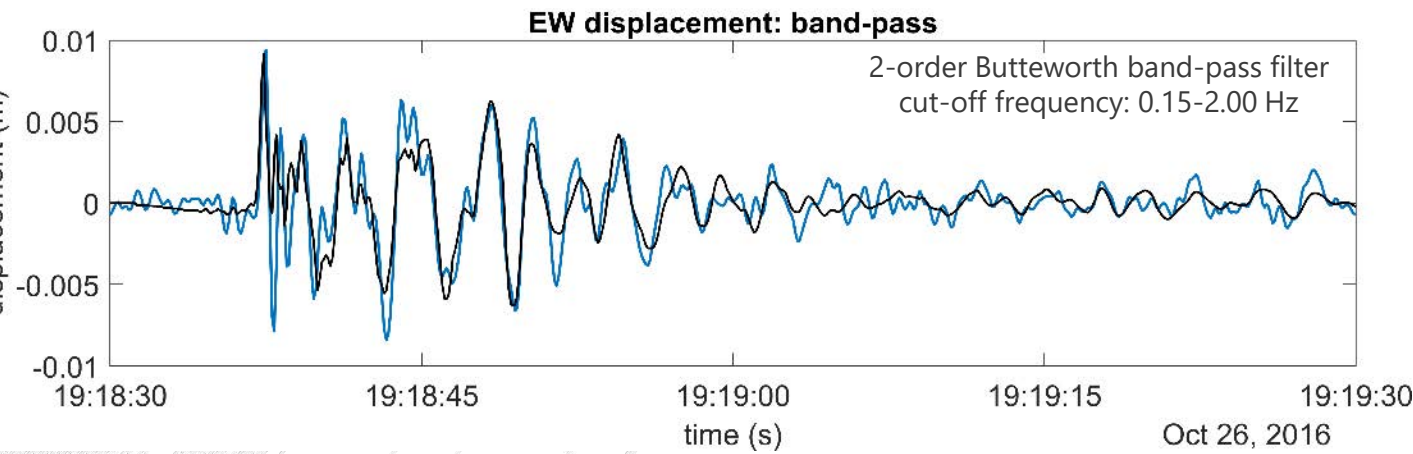
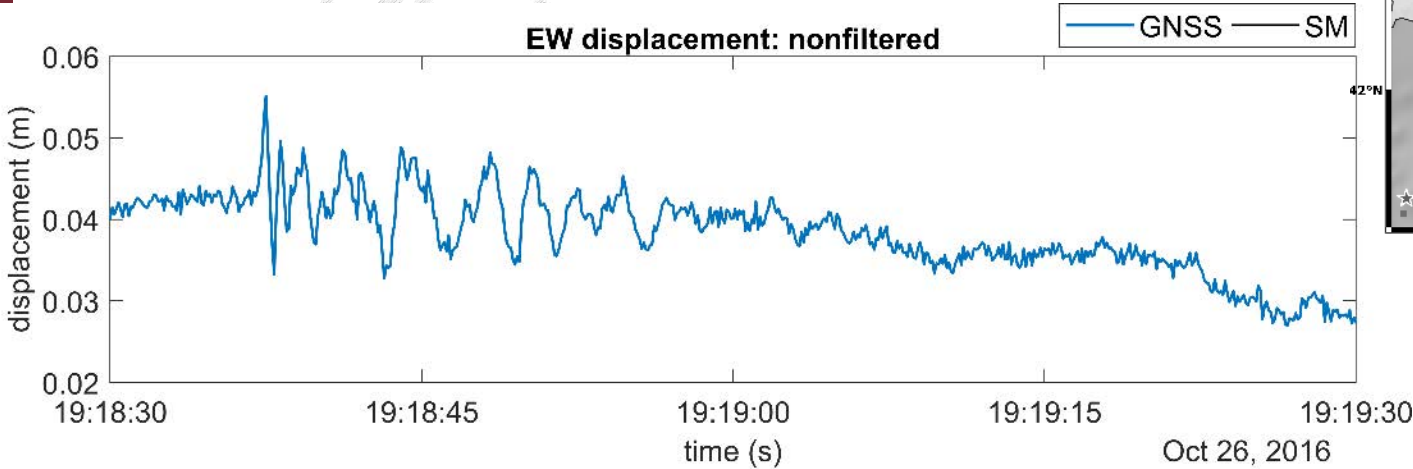
GPS: AMAT (10Hz);  
Accelerometer: AMT (200Hz)  
**EQ Norcia 2016-10-26**  
**19:18:08 UTC, Mw 6.6**  
**RTKlib 2.4.3**  
**CLK(5sec)+EPH+ERP+DCB**



# HR-GNSS vs SM -example



GPS: AMAT (10Hz);  
 Accelerometer: AMT (200Hz)  
**EQ Norcia 2016-10-26**  
**19:18:08 UTC, Mw 6.6**  
**RTKlib 2.4.3**  
**CLK(5sec)+EPH+ERP+DCB**



## Correlation coefficient GPS-SM

	-	HPass	BPass
'E'	0.36	0.74	0.80
'N'	0.30	0.65	0.73
'U'	0.30	0.72	0.82

## RMS GPS

	-	HPass	BPass
'E'	0.037	0.002	0.002
'N'	0.127	0.002	0.002
'U'	0.207	0.003	0.003

## Peak to peak amplitude

	-	HPass	BPass	SM
'E'	0.028	0.022	0.018	0.015
'N'	0.024	0.020	0.017	0.014
'U'	0.041	0.023	0.024	0.018

(Kudracik et al., 2019)

# Korelacja szeregów czasowych pozycji HR-GPS i SM

EQ	sensors	distance [km]		cut-off [Hz]		CORRELATION COEFFICIENTS								
						nonfiltered GPS time series			band-pass filtered GPS time series			percentage change		
						GPS/SM	epicentral	GPS/SM	low	high	E	N	U	E
Gorkha	KKN4/KATN	68.0	10.5	0.03	0.40	0.44	0.34	0.43	0.70	0.87	0.96	38%	61%	55%
	NAST/KATN	81.7	6.3	0.03	0.40	0.63	0.40	0.51	0.79	0.90	0.92	20%	55%	45%
Visso	ACCU/ACC	25.4	0.08	0.05	2.00	0.61	0.27	0.22	0.95	0.39	0.77	36%	31%	72%
	AMAT/AMT	33.7	0.8	0.15	1.50	0.73	0.19	0.67	0.80	0.52	0.78	8%	63%	14%
	GUMA/GUMA	24.0	0.5	0.15	2.00	0.87	0.71	0.81	0.96	0.78	0.82	9%	9%	2%
	MTER/RM33	44.9	0.4	0.15	1.00	0.37	0.20	0.33	0.80	0.57	0.49	54%	65%	32%
Norcia	ACCU/ACC	18.5	0.08	0.05	2.00	0.82	0.26	0.57	0.96	0.78	0.75	14%	67%	24%
	AMAT/AMT	26.8	0.9	0.10	1.50	0.72	0.57	0.66	0.77	0.67	0.67	7%	15%	1%
	ATTE/ATTE	74.0	0.4	0.05	1.50	0.89	0.23	0.66	0.93	0.34	0.67	4%	33%	1%
	CAPE/CPS	81.8	0.05	0.05	1.00	0.84	0.59	0.58	0.94	0.72	0.72	11%	18%	19%
	LTNA/LAT	152.4	0.6	0.05	1.00	0.96	0.82	0.37	0.99	0.90	0.40	3%	8%	8%
	MUVI/T1216	10.2	2.1	0.05	1.00	0.62	0.40	0.31	0.84	0.60	0.59	26%	33%	47%

Mean correlation coefficient:

0.55



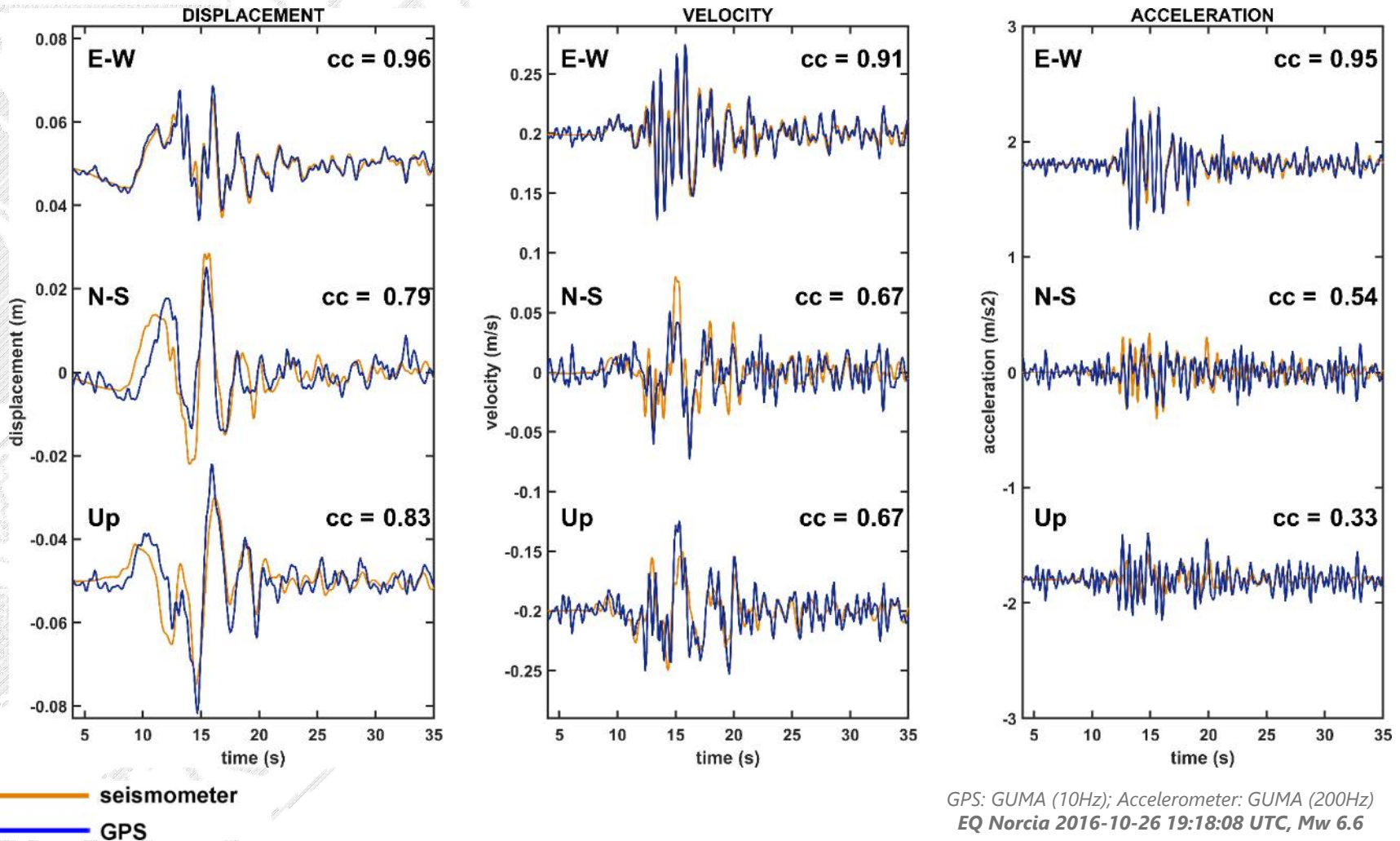
0.75

+27%



# HR-GPS/SM displacement, velocity, acceleration comparison

2-order Butterworth band-pass filter  
cut-off frequency: 0.05-2.00 Hz



GPS: GUMA (10Hz); Accelerometer: GUMA (200Hz)  
EQ Norcia 2016-10-26 19:18:08 UTC, Mw 6.6

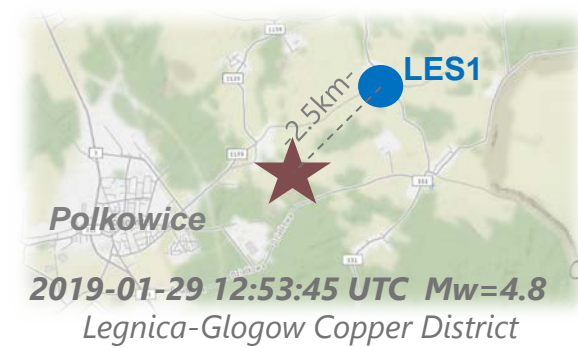
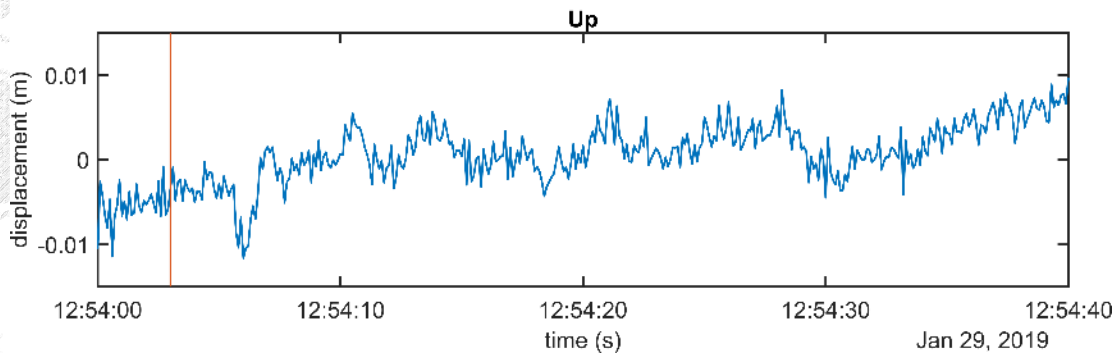
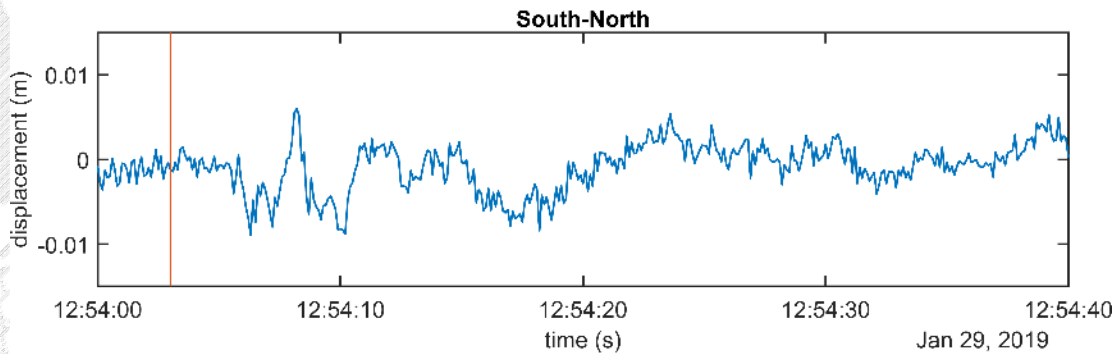
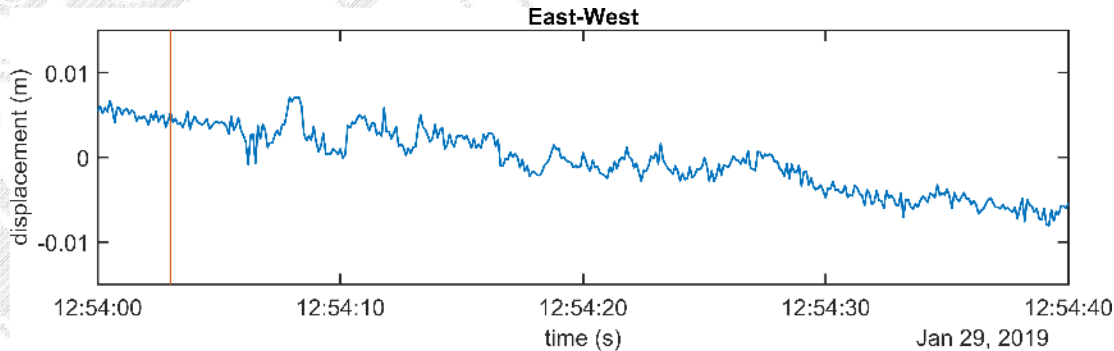


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The application of HR-GNSS in mining tremor analysis

# Mining tremor analysis with HR-GNSS

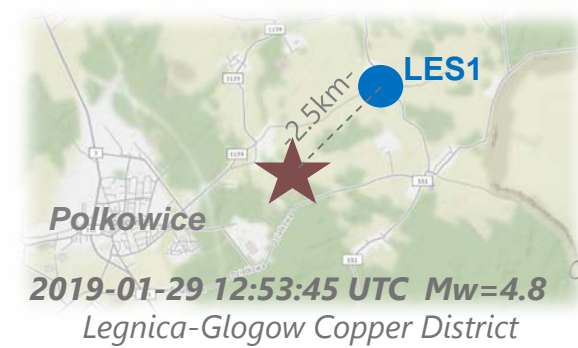
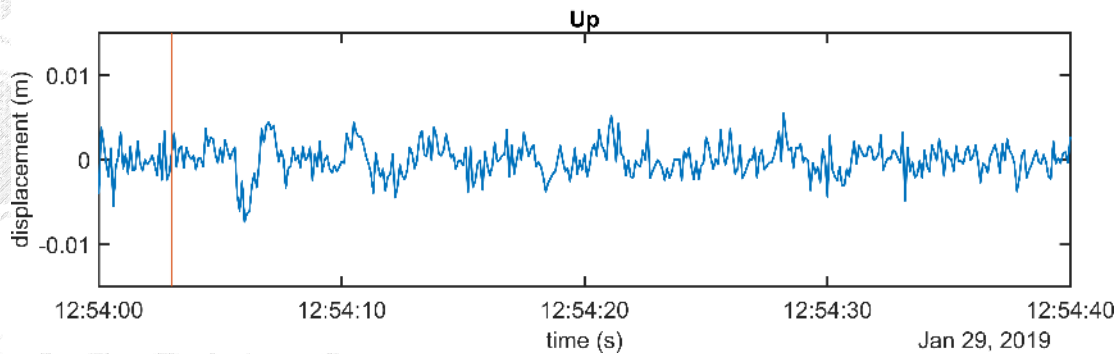
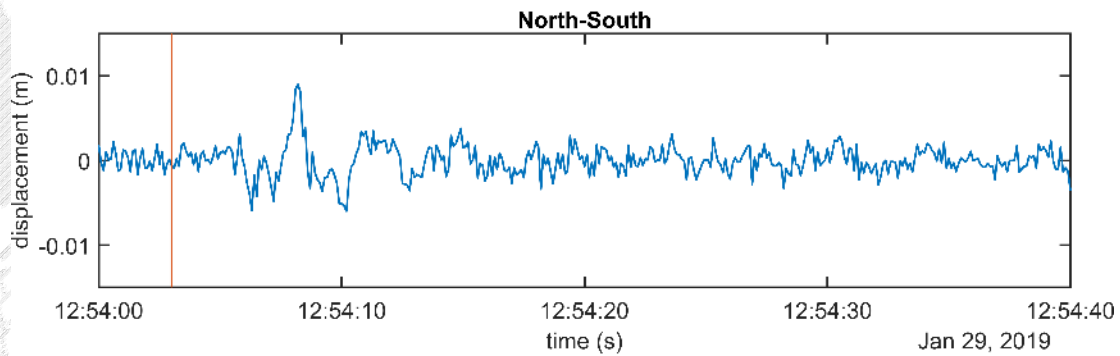
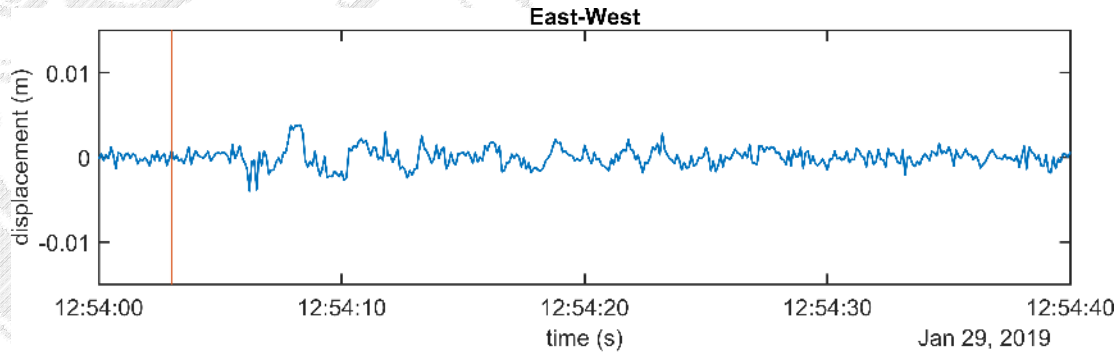
Nonfiltered displacements; GNSS station: LES1



# Mining tremor analysis with HR-GNSS

High-pass filtered displacements; GNSS station: LES1

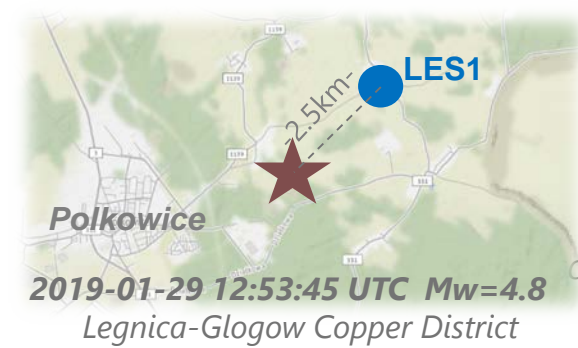
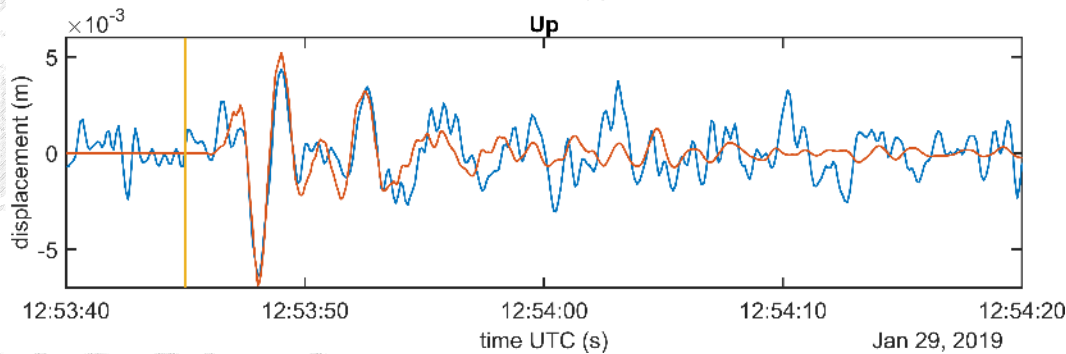
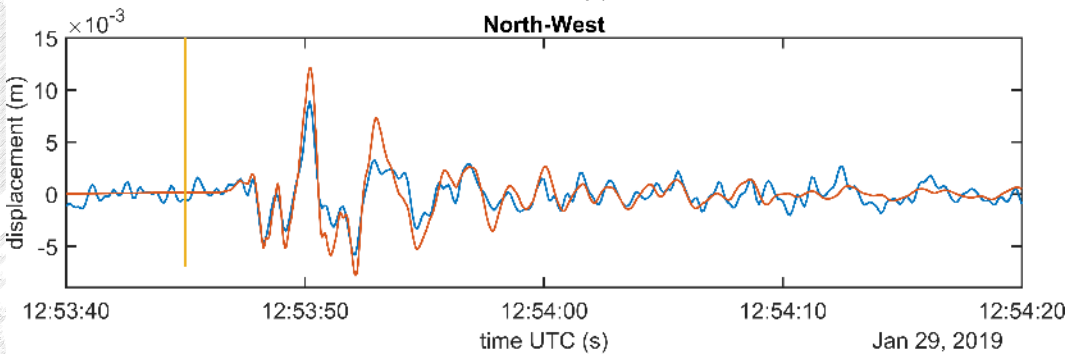
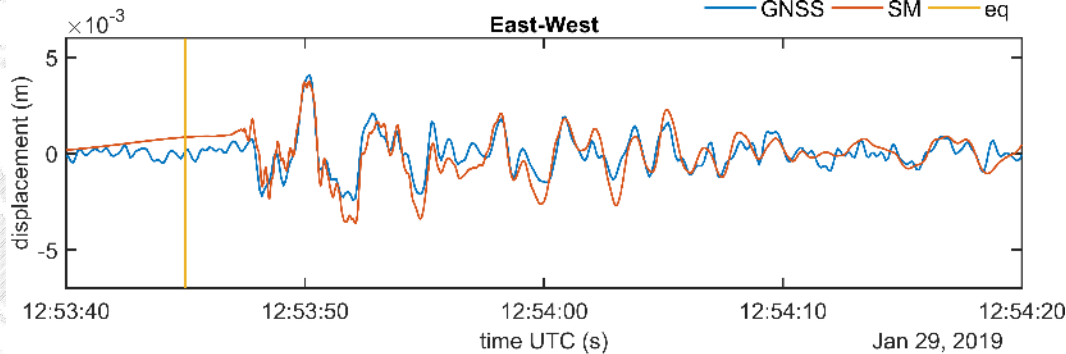
cut-off frequency: 0.17 Hz



# Mining tremor analysis with HR-GNSS

Band-pass filtered displacements; GNSS station: LES1

cut-off frequency: 0.17-2.00 Hz



correlation coefficient	
'E'	0.82
'N'	0.86
'U'	0.65

	maxSM	minSM	maxGNSS	minGNSS
'E'	0.004	-0.004	0.004	-0.002
'N'	0.012	-0.008	0.009	-0.006
'U'	0.005	-0.007	0.004	-0.006

max-min difference	SM	GNSS
'E'	0.007	0.007
'N'	0.020	0.015
'U'	0.012	0.011

## Future plans

- To continue the work on eliminating HR-GNSS errors to increase the precision of displacement time series
- To continue frequency analysis of time series of positions obtained from HR-GNSS
- To optimize of HR-GNSS data processing and determine the integration capabilities of HR-GNSS and seismological data to study small and medium natural and anthropogenic seismic events.